

Combination of Anns and Heuristic Algorithms in Modelling and Optimizing of Fenton Processes for Industrial Wastewater Treatment

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1 Combination of ANNs and heuristic algorithms in modelling and 2 optimizing of Fenton processes for industrial wastewater treatment

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15 16 **ABSTRACT**

17 In this study, it is aimed to evaluate COD removal performance of Classical-Fenton and
18 Photo-Fenton Processes from cosmetic wastewater by different prediction models. Besides
19 Response Surface Methodology (RSM), three neural networks were used to more reliably and
20 effectively predict the behavior of dependent variable at different values of relevant
21 parameters. These neural networks; multi-layer perceptron trained by Levenberg-Marquardt
22 (MLP-LM); multi-layer perceptron and single multiplicative neuron model trained by particle
23 swarm optimization algorithm (MLP-PSO; SMN-PSO). H₂O₂ doses, Fe(II) doses, and
24 H₂O₂/Fe(II) rates were independent variables of prediction models to optimize both processes
25 in batch reactors. The generated predictions for whole data set were compared with each
26 other. The prediction performances of models were evaluated by RMSE and MAPE error
27 criteria. Regression analysis was also applied to determine the performance of the best model.
28 The results obtained from all prediction tools showed that the model produces the best
29 predictive results in almost all cases is SMN-PSO model in terms of both criteria. In addition,
30 the genetic algorithm was utilized for SMN-PSO model results to find the optimum values of
31 the study. Thus, without the need to perform many different experiments, the optimum
32 parameter values can be determined to get maximum removal ratios.

33
34 **Keywords:** Fenton process, Multilayer Perceptron, Single Multiplicative Neuron Model,
35 Particle Swarm Optimization, Genetic Algorithm, RSM.

36 37 **1. Introduction**

38 One of the significant sources of environmental pollution is industrial wastewaters. The
39 consumption of freshwater used during production is also increasing with industrial
40 developments (Friha et al. 2014). The production of wastewater in the cosmetic industry is
41 excessively important such as in other industries. In addition to the wastewater generated
42 during the production of products, large amounts of wastewater are also released during the
43 cleaning process of reactors, pipes, filling lines, and other mechanical equipment used in the

44 production of products (de Andrade et al. 2020). The cosmetic industry can be divided into
45 five groups: haircare, make-up, skincare, fragrances, and others (Melo et al. 2013). The
46 wastewaters from cosmetic industries contain a high concentration of low biodegradability
47 organic compounds, suspended solids, fats and oils, natural oils, surfactants, solvents,
48 cosmetic ingredients, fragrances, colorants, dyes, bleaches, sunscreen agents, polymers,
49 exfoliators, emollients, chelating agents, UV filters, antioxidants, pH adjusters, and several
50 chemical compounds (Bautista et al. 2007; Banerjee et al. 2016; Bom et al. 2019). The most
51 frequently detected compounds are the recalcitrant organic matter among these pollutants in
52 water sources, and other major pollutants, non-ionic and anionic surfactants have been
53 determined in river water, groundwater, etc, and in their sediments and biota samples in the
54 world (Banerjee et al. 2016). For this reason, the toxicity of cosmetic wastewater should be
55 eliminated or reduced to acceptable limits require before discharging to receiving
56 environments.

57 Chemical and biological treatment technologies have been applied to treat cosmetic
58 wastewater. The most investigated technologies have also been coagulation/flocculation (El-
59 Gohary et al. 2010), dissolved ozone flotation (Wiliński et al. 2017), electro-coagulation,
60 membrane systems (Monsalvo et al. 2014), submerged membrane bioreactor (Friha et al.
61 2014), up-flow anaerobic sludge blanket reactor (Puyol et al. 2011), advanced oxidation
62 processes (AOPs) such as Fenton (Naumczyk et al. 2014) or photo-Fenton processes
63 (Muszyński et al. 2019), catalytic wet peroxide oxidation (Bautista et al. 2010), etc.
64 Compared to other treatment methods, AOPs are known as expensive methods due to their
65 high energy and chemical requirements (Oller et al. 2011). The common feature of AOPs
66 applied with different operating conditions is the formation of hydroxyl radicals at normal
67 pressure and room temperature. The hydroxyl radical is a non-selective and strong oxidant
68 that reacts with three different mechanisms. These mechanisms are hydrogen abstraction,
69 radical addition or electron transfer. Moreover, AOPs are always improving with new
70 equipment as well as the application of the most efficient methods (Paździor et al. 2019).
71 AOPs can be grouped as Fenton-based, Ozone-based, Photo-catalytic, EAOPs, and others.
72 Fenton-based processes among AOPs are Classical Fenton, Electro-Fenton, Photo-Fenton,
73 Sono-Fenton, Photo-Fenton/TiO₂, Photo-Sono-Fenton, Photo-Electro-Fenton, Sono-Electro-
74 Fenton. Fenton processes are preferred in the treatment of various wastewaters because of
75 their flexible operation, easy system, the ability to react at wide temperature ranges and under
76 atmospheric pressure (Fernandes et al. 2018).

77 The efficient use of treatment methods depends on determining the optimum operating
78 conditions. A limited number of trials are carried out with the experiment sets created for this
79 purpose and the optimum conditions are tried to be determined according to the data obtained
80 here. Recently, Artificial Neural Networks (ANNs) and Response Surface Methodology
81 (RSM) have come forward as effective experimental modelling and optimization methods,
82 especially for nonlinear systems. In literature, some approaches have been asserted to model
83 Fenton-based processes and to make predictions about these processes under certain
84 operational parameters. While most of these approaches include statistical-based models like
85 RSM, machine learning-based models such as ANNs have been started to apply as an
86 alternative modelling and prediction tool. Although ANNs are the subject of many studies for
87 time series prediction (Egrioglu et al. 2013; Cagcag Yolcu et al. 2018; Yolcu et al. 2019),

88 there are limited studies in the literature that use different ANN types to model Fenton-based
89 processes (Elmolla et al. 2010; Zarei et al. 2010; Jaafarzadeh et al. 2012; Sabour and Amiri
90 2017; Radwan et al. 2018; Baştürk and Alver 2019; Talwar et al. 2019; Tolba et al. 2019;
91 Gholizadeh et al. 2021). Modelling a dependent variable through certain independent
92 variables is essentially done to predict this dependent variable at different and especially non-
93 existent independent variable values. RSM is known as a traditional modelling and prediction
94 tool in literature. But, this traditional methodology has some limitations such as linear model
95 and distribution assumptions. The fundamental principle of linear modelling is that if the
96 relationships among variables are not linear, it gives a lower performance. This situation is
97 generally encountered in environmental sciences and ecological researches. Therefore, some
98 variables need to be converted (Lek et al. 1996). As the computer systems, ANNs are
99 improved to learn the data and to generate new information in an analogy to the human brain.
100 By means of its hidden layer, ANN learns the data structure and presents the suitable models.
101 ANNs are preferred to traditional methodology when programming is impossible or
102 exceedingly difficult.

103 The main goal of modelling in the present study is to predict the behavior of the
104 dependent variable in different values of the relevant parameters more reliably and
105 effectively. For this purpose, it is aimed to investigate and predict COD removal performance
106 of Classical and Photo-Fenton Processes from cosmetic wastewater by four different
107 prediction models. The first of the applied models is the traditional model, RSM. The second
108 is multi-layer perception (MLP) trained with the Levenberg-Marquardt training algorithm
109 (MLP-LM). And, MLP and Single Multiplicative Neuron Network trained by particle swarm
110 optimization algorithm (MLP-PSO; SMN-PSO) are also the distinctive models and innovative
111 aspect of this study.

112 In this study, the effects of H_2O_2 doses, Fe(II) doses, and $H_2O_2/Fe(II)$ rates were
113 determined as independent variables to optimize both Fenton processes in a batch reactor. The
114 scopes of the study were as follows: (i) to demonstrate the generalized abilities of models via
115 training, validation, and test; (ii) to evaluate the model performances by RMSE and MAPE
116 criteria; (iii) to do a comprehensive comparison of model results, (iv) to determine the
117 performance of the best model by regression analysis; (v) to obtain optimal values of the best
118 model by genetic algorithm; (vi) to compare the removal performances of Fenton processes.

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120

121 **2. Materials and Methods**

122 *2.1. Materials*

123 The cosmetic wastewater from the production of automobile care products was supplied
124 from a company in Nevşehir city of Turkey. The automobile care products produced in this
125 company are car washing shampoos, multi-purpose cleaning products, tire care/cleaning
126 products, car waxes, lubricants for car care, air conditioning care/cleaning products, special
127 cleaning products for rim care, brake pad cleaners. The real wastewater samples were taken as
128 2-hour composite samples into 5 L of bottles, brought to the laboratory by a storage box, and
129 stored in the refrigerator at 4°C. The main properties of this wastewater were determined and
130 were given in Table 1.

131

132 **Table 1.** The main properties of wastewater

| Parameters | Values | Parameters | Values |
|---------------------------|--------|----------------|--------|
| Temperature (°C) | 20.5 | Color (420 nm) | 1371 |
| pH | 7.48 | Color (485 nm) | 1262 |
| E. Conductivity (µs/cm) | 1782 | Color (508 nm) | 1235 |
| Dissolved oxygen (mg/L) | 4.3 | COD (mg/L) | 1128.9 |
| Orthophosphate (mg/L) | 0.63 | Sulfate (mg/L) | 544.6 |
| Anionic surfactant (mg/L) | 1.09 | | |

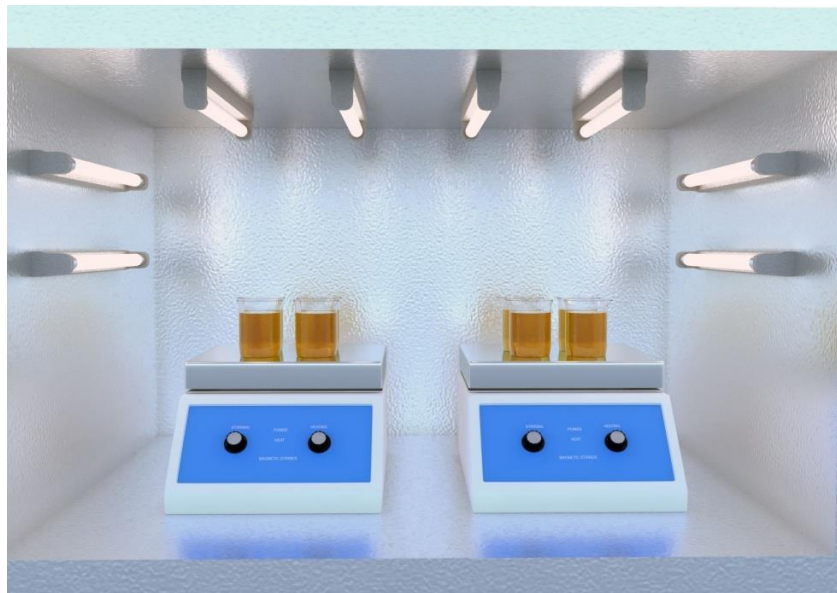
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134 *2.2. Experimental procedure*

135 The Photo-Fenton system has four main parts. As it is seen in Figure 1, the system
 136 consists of UV-C radiation lamps of 8 watts mounted parallelly, two magnetic stirrers (Mtops
 137 MS200), 500 mL of reactors, and a light-proof wooden cabin. The dimensions of the cabin are
 138 50 cm x 50 cm x 42 cm (L x W x H). The Classical-Fenton system consists of a 500 mL of
 139 reactor and a Jar Test Flocculator (Velp JLT6). Both processes were conducted in a batch
 140 system with 200 mL of wastewater samples. The influences of Fe(II) dose, H₂O₂ dose, and
 141 H₂O₂/Fe(II) rates on COD removal were investigated by both Fenton processes. The
 142 wastewater sample and reagents were mixed firstly at 300 rpm for two minutes. Then, mixing
 143 speed was decreased at 90 rpm and mixed for 45 minutes in Classical-Fenton reactors and 20
 144 min in Photo-Fenton reactors. All experiments were performed in the room temperature. After
 145 the precipitation process, the mixture was filtered by using 0.45 µm of membrane filters and
 146 COD concentration was analyzed by Closed Reflux Method by using a thermoreactor-Hach
 147 LT200 and a spectrophotometer-Hach DR3900 according to the standard method (Baird et al.
 148 2017). E. conductivity and pH were measured by a multi-meter during experiments (Hach
 149 HQ40d). COD removal performances are calculated as follows:

$$Removal\ efficiency(\%) = \frac{C_i - C_f}{C_i} \times 100 \quad (1)$$

150 where C_f and C_i are the final and inlet COD concentrations (mg/L), respectively.



151

152 **Fig. 1.** A schematic representation of Photo-Fenton Process

153

154 2.3. Multi-Layer Perceptron Neural Networks

155 Feed-forward neural networks are one of the most popular architectures owing to their
156 structural flexibility, capabilities of well-representational, and a large number of training
157 algorithms available as well as well-known machine learning (Haykin 1999). They are
158 basically designed to replicate the ability for creating and designing new information of the
159 human brain. MLP was firstly proposed by Werbos with the intention of solving the nonlinear
160 problems due to its architectural structure including hidden layer(s) (Werbos 1974). Then,
161 Rumelhart et al. were improved MLP methods (Rumelhart et al. 1986). MLP methods have
162 been widely used for so many areas such as prediction, classifications, modelling etc. This
163 network comprises neurons regulated in layers as input, outputs, and one or more hidden
164 layers. Every neuron is attached to all neurons of the next layer. A number of neurons in the
165 hidden layer have a crucial effect on the performance of the network (Li et al. 2017). Having a
166 data-driven feature that comes from including hidden layers in its structure enables these
167 kinds of neural networks to have flexible and adaptable models for nonlinear problems. The
168 neurons are attached by weights and output signals that are a function of the sum inputs to the
169 neurons modified by a simple nonlinear transfer, or activation function.

170

171 2.4. Single Multiplicative Neuron Model

172 Single multiplicative neuron model (SMN) was firstly introduced to the literature by
173 Yadav. et al. (Yadav et al. 2007). SMN structure has just one neuron as a hidden layer, unlike
174 the MLP. Having this feature makes SMN more advantageous, especially in solving the
175 determination of appropriate structure problems for MLP. In SMN structure, there is only one
176 neuron in the model and instead of an addition operator; the process of multiplication is
177 applied to the signal accruing to the neuron. In Eq.(1), $\Omega(x, \Theta)$ function comprises of the
178 product of weighted inputs. Θ is a vector which include the weights (w_j), X_{ij} is i th sample for
179 j th input, and the biases (b_j) of the model and can be shown with $\Theta = (w_1, w_2, \dots, w_m, b_1, b_2,$
180 $\dots, b_m)$. There are m inputs which are showed with (X_1, X_2, \dots, X_m) and just one output given
181 by y and also f shows the activation function which is the function that specifies the nonlinear
182 relationships between inputs and output. The net value of the neuron is calculated as:

$$183 \quad net_i = \Omega(x, \Theta) = \prod_{j=1}^m (w_j X_{ij} + b_j), \quad i = 1, 2, \dots, n \quad (1)$$

$$184 \quad y_i = f(net_i) \quad i = 1, 2, \dots, n \quad (2)$$

183

184 2.5. Particle Swarm Optimization

185 PSO is a kind of heuristic optimization method, proposed firstly by Kennedy and
186 Eberhart (Kennedy and Eberhart 1995). PSO was improved by adding some coefficients to
187 the optimization process (Shi and Eberhart 1999; Ma et al. 2006). The most significant
188 feature of this algorithm is the ability to reach the optimum point from several points at the
189 same time. So, having this feature gives the opportunity to PSO algorithm to reach global
190 optimum by escaping local optimum. Because of its high solution quality, simplicity, and
191 good convergence properties, recently, the PSO algorithm has been widely applied to the data.
192 In the PSO method, each particle has a position and speed that represents the solution to the
193 optimization problem and the search direction in the search space. While the best positions of

194 particles are stored in *Pbest* vectors, the best state of all particles is stored in *Gbest* vectors
 195 representing the global optimum.

196 In this study to be able to train the SMN, modified PSO is utilized. The process of
 197 modified PSO analysis has some steps which differentiate this model from the traditional one.
 198 These are cognitive (c_1) and social (c_2) coefficients, the inertia parameter (w). These
 199 parameters are calculated for each iteration by using the following equations.

$$c_1 = (c_{1f} - c_{1i}) \frac{t}{maxt} + c_{1i} \quad (3)$$

$$c_2 = (c_{2f} - c_{2i}) \frac{t}{maxt} + c_{2i} \quad (4)$$

$$w = (w_2 - w_1) \frac{maxt - t}{maxt} + w_1 \quad (5)$$

200

201 Here, (c_{1i} , c_{1f}) are possible intervals for cognitive coefficients, (c_{2i} , c_{2f}) are ranges for
 202 social coefficients and (w_1 , w_2) are inertia parameters. *maxt* gives a maximal number of
 203 iterations, and t is a valid iteration number. And finally, new values of positions and velocities
 204 are calculated with equations given below;

205

$$V_{id}^{k+1} = [w \times V_{id}^k + c_1 \times rand_1 \times (Pbest_{id} - X_{id}) + c_2 \times rand_2 \times (Gbest - X_{id})] \quad (6)$$

$$X_{id}^{k+1} = X_{id} + V_{id}^{k+1} \quad (7)$$

206

207 where $rand_1$ and $rand_2$ are random numbers between 0 and 1. After reaching the
 208 predetermined iteration number, *Gbest*'s results are taken optimal parameters of the system.

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211 2.6. Genetic Algorithm

212 Genetic algorithm (GA) was presented by Holland (Holland 1992) and improved by
 213 Goldberg (Goldberg 1989). GA is one of the heuristic optimization methods used to find
 214 benefit solutions to complicated problems. It contains important parts as the population for
 215 selection, crossover, and mutation. Firstly, some random solutions (individuals) that are each
 216 containing several features (chromosomes) are created in the algorithm. According to the laws
 217 of genetics, cross-over and mutations happen in chromosomes to create the second generation
 218 of individuals with more different properties. The calculations for GA function were
 219 performed through MATLAB 2018b.

220

221 3. Results and discussions

222 In this study, it is basically aimed to predict COD removal performance of Classical and
 223 Photo-Fenton Processes from cosmetic wastewater by using a traditional method (RSM) and
 224 three state-of-the-art models (MLP-LM, MLP-PSO, and SMN-PSO). The experiment design
 225 properties of Classical and Photo-Fenton Processes are summarized in Table 2. A scheme of
 226 the combination of ANNs and heuristic algorithms is presented in Fig.2.

Table 2. The experimental conditions and architectures of neural networks

| Expr. No | Fenton process | Independent Variables | Fixed Variables | MLP Architecture | SMN Architecture |
|----------|----------------|--|--|------------------------|------------------|
| 1 | Classic | A. Fe(II) dose (50-400 mg/L) B. H ₂ O ₂ dose (600 mg/L, 900 mg/L) | 1. pH/3 2. Temperature/23±2°C 3. Fast mixing speed/300 rpm 4. Slow mixing speed/90 rpm | from 2-1-1 to 2-4-1 | 2-1-1 |
| 2 | Photo | A. Fe(II) dose (50-400 mg/L) B. H ₂ O ₂ dose (600 mg/L, 900 mg/L) | 1. pH/3 2. Temperature/23±2°C 3. Fast mixing speed/300 rpm 4. Slow mixing speed/90 rpm | from 2-1-1 to 2-4-1 | 2-1-1 |
| 3 | Classic | A. H ₂ O ₂ dose (200-1050 mg/L) B. Fe(II) dose (150 mg/L, 300 mg/L, 400 mg/L) | 1. pH/3 2. Temperature/23±2°C 3. Fast mixing speed/300 rpm 4. Slow mixing speed/90 rpm | from 2-1-1 to 2-4-1 | 2-1-1 |
| 4 | Photo | A. H ₂ O ₂ dose (200-1050 mg/L) B. Fe(II) dose (150 mg/L, 300 mg/L, 400 mg/L) | 1. pH/3 2. Temperature/23±2°C 3. Fast mixing speed/300 rpm 4. Slow mixing speed/90rpm | from 2-1-1 to 2-4-1 | 2-1-1 |
| 5 | Classic | A. H ₂ O ₂ dose (200-1050 mg/L) B. Fe(II) dose (50-400 mg/L) | 1. pH/3 2. Temperature/ 23±2°C 3. Fast mixing speed/300 rpm 4. Slow mixing speed/90rpm | from 2-1-1 to 2-4-1 | 2-1-1 |
| 6 | Photo | A. H ₂ O ₂ dose (200-1050 mg/L) B. Fe(II) dose (50-400 mg/L) | 1. pH/3 2. Temperature/23±2°C 3. Fast mixing speed/300 rpm 4. Slow mixing speed/90 rpm | from 2-1-1 to 2-4-1 | 2-1-1 |
| 7 | Classic | A. Contact time (0-60 min) B. Fe(II) dose (150 mg/L, 400 mg/L) | 1. pH/3 2. Temperature/23±2°C 3. Fast mixing speed/300 rpm 4. Slow mixing speed/90 rpm 5.H ₂ O ₂ dose/900 mg/L | from 2-1-1 to 2-4-1 | 2-1-1 |
| 8 | Photo | A. Contact time (0-60 min) B. Fe(II) dose (300 mg/L) | 1. pH/3 2. Temperature/23±2°C 3. Fast mixing speed/300 rpm 4. Slow mixing speed/90 rpm 5.H ₂ O ₂ dose/600 mg/L | from 2-1-1 to 2-4-1 | 2-1-1 |

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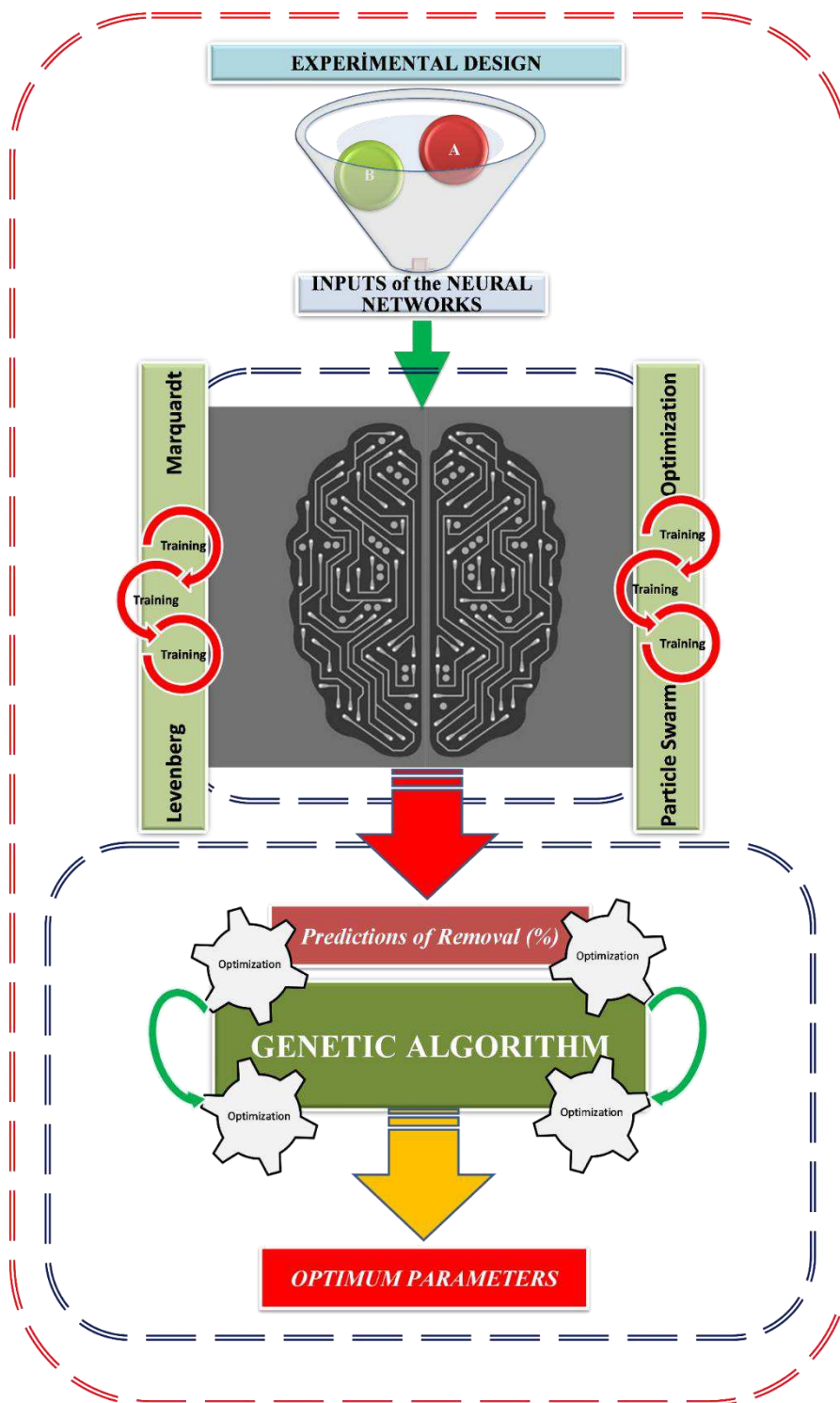
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237 **Fig.2.** A scheme of the combination of ANNs and heuristic algorithms

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239 *3.1. Performance measures*

240 The prediction results produced from RSM, MLP-LM, MLP-PSO, and SMN-PSO
 241 models were evaluated from different perspectives. Firstly, RMSE and MAPE that is revealed
 242 the predictive performance of models, the basic statistical criteria widely applied in prediction
 243 literature were discussed.

$$RMSE = \sqrt{\frac{1}{n} \sum_{p=1}^n (Target_p - Output_p)^2} \quad (8)$$

$$MAPE = \text{mean} \left(\left| \frac{Target_p - Output_p}{Target_p} \right| \right), p = 1, 2, \dots, n \quad (9)$$

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The other perspective one is the analysis of the regression model to be created for the predictions and target values, and some properties of this regression model which is given by Eq. (10). For a successful prediction tool, the regression and determination coefficients of the model are expected to be equal to 1 or quite close to 1. In addition, scatter diagrams showing the symphony between predictions and actual values were illustrated.

$$Y_t = \beta \hat{Y}_t + \varepsilon_t \quad (10)$$

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3.2. RSM modelling and optimization

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This study contains basic information rather than detailed information about RSM since it is a well-known statistical method. The second-order polynomial model structure for the case where there are k independent variables is written as:

$$RE(\%) = \beta_0 + \sum_{i=1}^k \beta_i X_i + \sum_{i=1}^k \beta_{ii} X_i^2 + \sum_{i=1}^k \sum_{i \neq j=1}^k \beta_{ij} X_i X_j + \varepsilon \quad (11)$$

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For all experiment designs including Classical and Photo-Fenton Processes, the results of the determined data in terms of un-coded factors using RSM are given in Table 3. Considering the results given in Table 1, it is seen from the MAPE values that the predictions obtained by RSM in 5 of 8 experiments contain approximately 5% or more error. On the other hand, the percentage error was around 4% for 3rd experiment, while it was 2.5% for the 7th experiment and 1.33% for the 8th experiment. Considering R^2 -value, which is another measure of the success of the model, it is seen that relatively high R^2 values (higher than 90%) are obtained for 2nd, 7th and 8th experiments in parallel with the MAPE values.

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272 **Table 3.** The RSM results for the experiments

| Exp. No | Optimized Model (by omitting insignificant terms) | Optimal Values | y | d | $R^2(\%)$ | RMSE | MAPE |
|---------|--|--------------------------|---------|--------|-----------|--------|----------|
| 1 | $\widehat{RE} = 6.1 + 0.4036A - 0.000605A^2$ | A. 329.293 B. 900 | 84.4790 | 0.7782 | 92.98 | 4.4125 | 6.4823% |
| 2 | $\widehat{RE} = 25.04 + 0.3072A - 0.000382A^2$ | A. 400 B. 900 | 88.8368 | 0.8161 | 96.74 | 2.8959 | 3.9062% |
| 3 | $\widehat{RE} = -14.4 + 0.1396A + 0.0250B - 0.000071A^2$ | A. 1027.96 B. 400 | 74.9213 | 0.6828 | 91.56 | 4.9924 | 8.3217% |
| 4 | $\widehat{RE} = 10.4 + 0.0628A + 0.1243B$ | A. 1050 B. 400 | 87.4843 | 0.8063 | 89.46 | 4.4770 | 6.1295% |
| 5 | $\widehat{RE} = -71.9 + 0.2434A + 0.3373B - 0.000156A^2 - 0.000588B^2$ | A. 826.768 B. 322.222 | 82.9769 | 0.7847 | 86.31 | 7.1229 | 11.5837% |
| 6 | $\widehat{RE} = -6.9 + 0.1027A + 0.1947B - 0.000068A^2 - 0.000384B^2 + 0.000107AB$ | A. 1050 B. 399.015 | 86.9010 | 0.7973 | 84.10 | 5.9786 | 7.1423% |
| 7 | $\widehat{RE} = 28.54 + 1.669A + 0.03699B - 0.01608A^2$ | A. 52.222 B. 400 | 87.1502 | 0.7868 | 98.15 | 1.8424 | 2.4908% |
| 8 | $\widehat{RE} = 39264 + 1.479A - 0.01518A^2$ | A. 48.729 B. 300 | 90.4605 | 0.7439 | 97.82 | 1.4658 | 1.3340% |

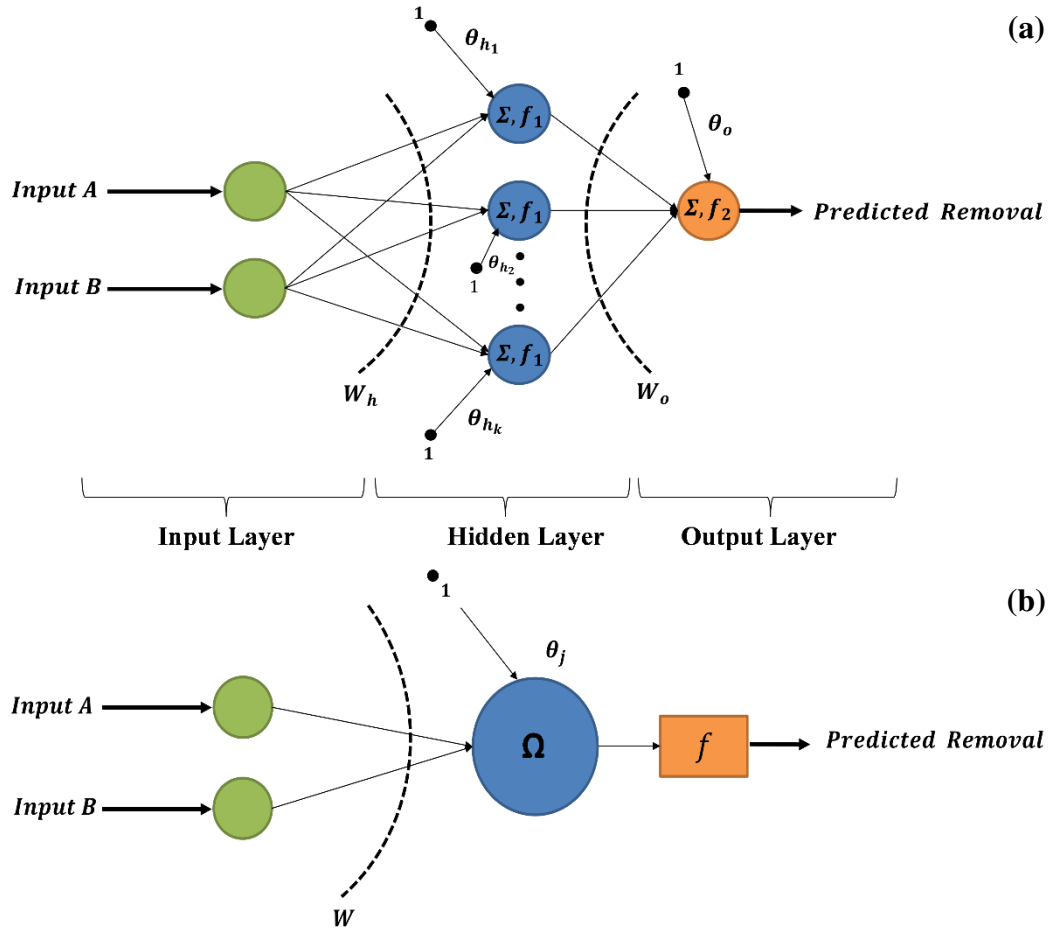
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275 *3.3. Neural networks-based modelling*

276 Artificial neural networks have been widely used in many scientific areas. In particular,
 277 thanks to the rapid development of computer technology in recent years, neural network-
 278 based prediction models have started to be used frequently. One of these models is the MLP-
 279 LM. While derivative-based training algorithms such as Levenberg-Marquardt learning
 280 algorithm could sometimes get stuck in local optimum, particle swarm optimization carries no
 281 such risk.

282 From this point of view, unlike existing studies in the literature that use MLP for similar
 283 purposes, MLP and SMN trained by PSO were used as prediction tools in this study. Unlike
 284 MLP, there is no architectural selection problem since SMN has only one neuron, making it
 285 more applicable. Moreover, using a multiplicative multiplication aggregation function instead
 286 of an additive aggregation function makes SMN more flexible and successful, especially in
 287 solving nonlinear problems. The use of SMN, which has these features, as a predictive tool in
 288 this field is another pioneering and distinguishing feature of this study compared to other
 289 studies in the literature. In this respect, this study is the first study that takes into account all
 290 the above mentioned issues in its literature. Also, analysis and modelling using MLP-LM,
 291 MLP-PSO, and SMN-PSO were performed with MATLAB program codes created by
 292 researchers of this study. MLP and SMN structures with the two inputs are given in Figure 3.



293 **Fig. 3.** An illustration of MLP structure / 2-k-1 Architecture (a) and SMN structure (b)

294 For all experiment designs of Classical and Photo-Fenton Processes, the prediction results
 295 produced by MLP-LM, MLP-PSO, and SMN-PSO models are given in Table 4 and Table 5,
 296 in terms of RMSE and MAPE criteria, respectively. These tables also give the success
 297 rankings of the prediction models according to the corresponding criteria. When the findings
 298 given in Tables 4 and 5 were evaluated, it was seen that all three NN-based prediction models
 299 produced better predictive results than the RSM in all cases except for one exception, in terms
 300 of both criteria. Among these three NN-based models, it is seen that SMN-PSO was the model
 301 that produced the best prediction results, as expected, according to the average success
 302 rankings created for both criteria. The main reason for this situation is that SMN-PSO trained
 303 by PSO has less risk of getting stuck in local optimums than MLP-LM trained with
 304 Levenberg-Marquardt algorithm.

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310 **Table 4.** The prediction results in terms of RMSE

| Case | Processes | # Samples | SMN-PSO | | MLP-PSO | | MLP-LM | | |
|---|--------------------------|------------|---------------|--------|----------|--------|----------|--------|----------|
| | | | RMSE | Rank | RMSE | Rank | RMSE | Rank | |
| Effect of Fe (II) doses | Classical-Fenton Process | 10 | Training | 1.7930 | 1 | 2.4818 | 2 | 2.9371 | 3 |
| | | 3 | Validation | 1.5488 | 1 | 1.6673 | 2 | 4.3519 | 3 |
| | | 3 | Test | 0.6645 | 1 | 0.7423 | 2 | 0.8924 | 3 |
| | | 16 | ALL | 1.5943 | 1 | 2.1152 | 2 | 3.0153 | 3 |
| | Photo-Fenton Process | 10 | Training | 1.7108 | 1 | 2.2669 | 3 | 2.0894 | 2 |
| | | 3 | Validation | 0.5633 | 1 | 1.5524 | 3 | 1.0260 | 2 |
| | | 3 | Test | 0.2093 | 1 | 0.3939 | 2 | 0.5513 | 3 |
| | | 16 | ALL | 1.3773 | 1 | 1.9217 | 3 | 1.7271 | 2 |
| Effect of H ₂ O ₂ doses | Classical-Fenton Process | 11 | Training | 1.7904 | 1 | 2.0809 | 2 | 2.6345 | 3 |
| | | 4 | Validation | 1.2094 | 2 | 1.7601 | 3 | 1.1319 | 1 |
| | | 4 | Test | 1.0630 | 1 | 1.5196 | 2 | 2.0760 | 3 |
| | | 19 | ALL | 1.5497 | 1 | 1.9093 | 2 | 2.2793 | 3 |
| | Photo-Fenton Process | 15 | Training | 1.1129 | 1 | 1.7680 | 2 | 2.4760 | 3 |
| | | 5 | Validation | 1.2857 | 3 | 1.2258 | 1 | 1.2715 | 2 |
| | | 5 | Test | 0.7732 | 1 | 0.9021 | 2 | 1.0530 | 3 |
| | | 25 | ALL | 1.0924 | 1 | 1.5293 | 2 | 2.0551 | 3 |
| Effect of H ₂ O ₂ /Fe(II) rates | Classical-Fenton Process | 19 | Training | 1.5455 | 1 | 1.7818 | 2 | 4.0121 | 3 |
| | | 5 | Validation | 1.5539 | 1 | 1.7180 | 2 | 1.8323 | 3 |
| | | 5 | Test | 0.9173 | 1 | 1.0169 | 2 | 1.8114 | 3 |
| | | 29 | ALL | 1.4581 | 1 | 1.5617 | 2 | 3.4192 | 3 |
| | Photo-Fenton Process | 25 | Training | 1.0027 | 1 | 1.5506 | 2 | 3.3785 | 3 |
| | | 5 | Validation | 0.9724 | 1 | 1.2980 | 2 | 3.7574 | 3 |
| | | 5 | Test | 0.6980 | 1 | 1.0178 | 2 | 2.8843 | 3 |
| | | 35 | ALL | 0.9606 | 1 | 1.4512 | 2 | 3.3702 | 3 |
| Effect of contact time | Classical-Fenton Process | 10 | Training | 1.1510 | 2 | 1.6974 | 3 | 0.7898 | 1 |
| | | 2 | Validation | 0.5010 | 2 | 0.3977 | 1 | 1.1039 | 3 |
| | | 2 | Test | 0.4060 | 2 | 0.2439 | 1 | 0.4436 | 3 |
| | | 14 | ALL | 1.0028 | 2 | 1.4454 | 3 | 0.8049 | 1 |
| | Photo-Fenton Process | 3 | Training | 0.8431 | 1 | 0.8520 | 2 | 1.8142 | 3 |
| | | 2 | Validation | 0.8725 | 1 | 1.2502 | 2 | 2.1566 | 3 |
| | | 2 | Test | 0.4968 | 1 | 1.0160 | 2 | 2.3276 | 3 |
| | | 7 | ALL | 0.7699 | 1 | 1.0260 | 2 | 2.0706 | 4 |
| Average | | Training | 1.1250 | | 2.2500 | | 2.6250 | | |
| | | Validation | 1.5000 | | 2.0000 | | 2.5000 | | |
| | | Test | 1.1250 | | 1.8750 | | 3.0000 | | |
| | | ALL | 1.1250 | | 2.2500 | | 2.7500 | | |

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Table 5. The prediction results in terms of MAPE

| Case | Processes | # Samples | SMN-PSO | | MLP-PSO | | MLP-LM | | |
|--|--------------------------|--------------|---------------|---------|----------|---------|----------|---------|----------|
| | | | MAPE | Rank | MAPE | Rank | MAPE | Rank | |
| Effect of Fe (II) doses | Classical-Fenton Process | 10 | Training | 3.1235% | 1 | 4.2101% | 2 | 5.4812% | 3 |
| | | 3 | Validation | 2.5373% | 1 | 2.9869% | 2 | 4.6784% | 3 |
| | | 3 | Test | 1.0634% | 1 | 1.1402% | 3 | 1.0784% | 2 |
| | | 16 | ALL | 2.6273% | 1 | 3.4052% | 2 | 4.5051% | 3 |
| | Photo-Fenton Process | 10 | Training | 2.2558% | 1 | 3.4481% | 3 | 2.3766% | 2 |
| | | 3 | Validation | 0.9992% | 1 | 2.2900% | 3 | 1.4986% | 2 |
| | | 3 | Test | 0.2051% | 1 | 0.5819% | 2 | 0.7329% | 3 |
| | | 16 | ALL | 1.6357% | 1 | 2.6935% | 3 | 1.9038% | 2 |
| Effect of H ₂ O ₂ doses | Classical-Fenton Process | 11 | Training | 2.7672% | 1 | 4.6369% | 3 | 2.9823% | 2 |
| | | 4 | Validation | 2.1089% | 1 | 2.5006% | 3 | 1.7866% | 2 |
| | | 4 | Test | 1.5827% | 1 | 1.6765% | 2 | 3.3245% | 3 |
| | | 19 | ALL | 2.3793% | 1 | 3.5639% | 3 | 2.8027% | 2 |
| | Photo-Fenton Process | 15 | Training | 1.6213% | 1 | 2.5519% | 3 | 2.3834% | 2 |
| | | 5 | Validation | 1.1778% | 1 | 1.6106% | 2 | 1.1670% | 3 |
| | | 5 | Test | 1.1082% | 1 | 1.3129% | 2 | 1.3742% | 3 |
| | | 25 | ALL | 1.4300% | 1 | 2.1159% | 3 | 1.9383% | 2 |
| Effect of H ₂ O ₂ /Fe (II) | Classical-Fenton Process | 19 | Training | 2.2681% | 1 | 3.0225% | 2 | 4.5416% | 3 |
| | | 5 | Validation | 2.0428% | 1 | 2.7955% | 2 | 3.8585% | 3 |
| | | 5 | Test | 1.3458% | 2 | 1.1457% | 1 | 2.7890% | 3 |
| | | 29 | ALL | 2.0702% | 1 | 2.5643% | 2 | 4.1217% | 3 |
| | Photo-Fenton Process | 25 | Training | 1.4591% | 1 | 2.2576% | 2 | 4.7201% | 3 |
| | | 5 | Validation | 1.3227% | 1 | 1.8462% | 2 | 4.9370% | 3 |
| | | 5 | Test | 1.0807% | 1 | 1.4088% | 2 | 4.3294% | 3 |
| | | 35 | ALL | 1.3855% | 1 | 2.0776% | 2 | 4.6953% | 3 |
| Effect of contact time | Classical-Fenton Process | 10 | Training | 1.7168% | 2 | 2.1805% | 3 | 0.9750% | 1 |
| | | 2 | Validation | 0.7531% | 2 | 0.5466% | 1 | 1.6131% | 3 |
| | | 2 | Test | 0.5132% | 2 | 0.2744% | 1 | 0.5944% | 3 |
| | | 14 | ALL | 1.4072% | 2 | 1.6748% | 3 | 1.0118% | 1 |
| | Photo-Fenton Process | 3 | Training | 0.9751% | 1 | 1.0655% | 2 | 1.6829% | 3 |
| | | 2 | Validation | 1.0624% | 1 | 1.5248% | 2 | 2.1396% | 3 |
| | | 2 | Test | 0.4825% | 1 | 1.1284% | 2 | 2.4598% | 3 |
| | | 7 | ALL | 0.8593% | 1 | 1.2147% | 2 | 2.0353% | 4 |
| Average | | Training | 1.1250 | | 2.5000 | | 2.3750 | | |
| | | Validation | 1.1250 | | 2.1250 | | 2.7500 | | |
| | | Test | 1.2500 | | 1.8750 | | 2.8750 | | |
| | | ALL | 1.1250 | | 2.5000 | | 2.5000 | | |

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In addition, SMN does not have architectural selection problems, and thanks to the multiplicative aggregation function it uses, it is more flexible and successful than MLP in these types of problems with non-linearity dominance. Thus, it is seen that the SMN-PSO produced predictive results with errors of around 2% and 3%, and in many cases much lower than these rates, up to values less than 1%, considering the training, validity, test sets and even all data sets for each experiment. Another important reason for preference to use NN-based prediction tools is that unlike RSM, producing in stronger results in terms of reliability and consistency by analyzing the data in different parts such as training, validation, and test

330 sets. Especially when considering estimates from out-of-sample test sets, the MAPE values
 331 were about 1% for almost all experiments. In 2nd, 7th and 8th experiments, the percentage
 332 errors even below 1% were observed in the out-of-sample data set for SMN-PSO. These
 333 findings indicate that SMN-PSO produces highly satisfactory and consistent predictions even
 334 for the out-of-sample data sets. One of the most important aspects of these results is that in
 335 cases that experimental designs are difficult or costly, satisfactory predictive results for out-
 336 of-sample data sets without the need for any additional experiments are proof that they can be
 337 produced with SMN-PSO.

338 Another way to reveal the superior predictive ability of a prediction tool is to examine
 339 some properties of a linear regression model to be established between predictions and target
 340 values. Such a strategy was also followed for SMN-PSO, which showed superior performance
 341 among the three NN-based prediction models. For the estimate of the regression coefficient
 342 ($\hat{\beta}$), a satisfactory and applicable prediction tool and also the coefficient of determination (R^2)
 343 of the model $Y_t = \beta \hat{Y}_t + \varepsilon_t$ are desired to be 1 or quite close to 1. Table 6 presents the findings
 344 for this regression analysis.

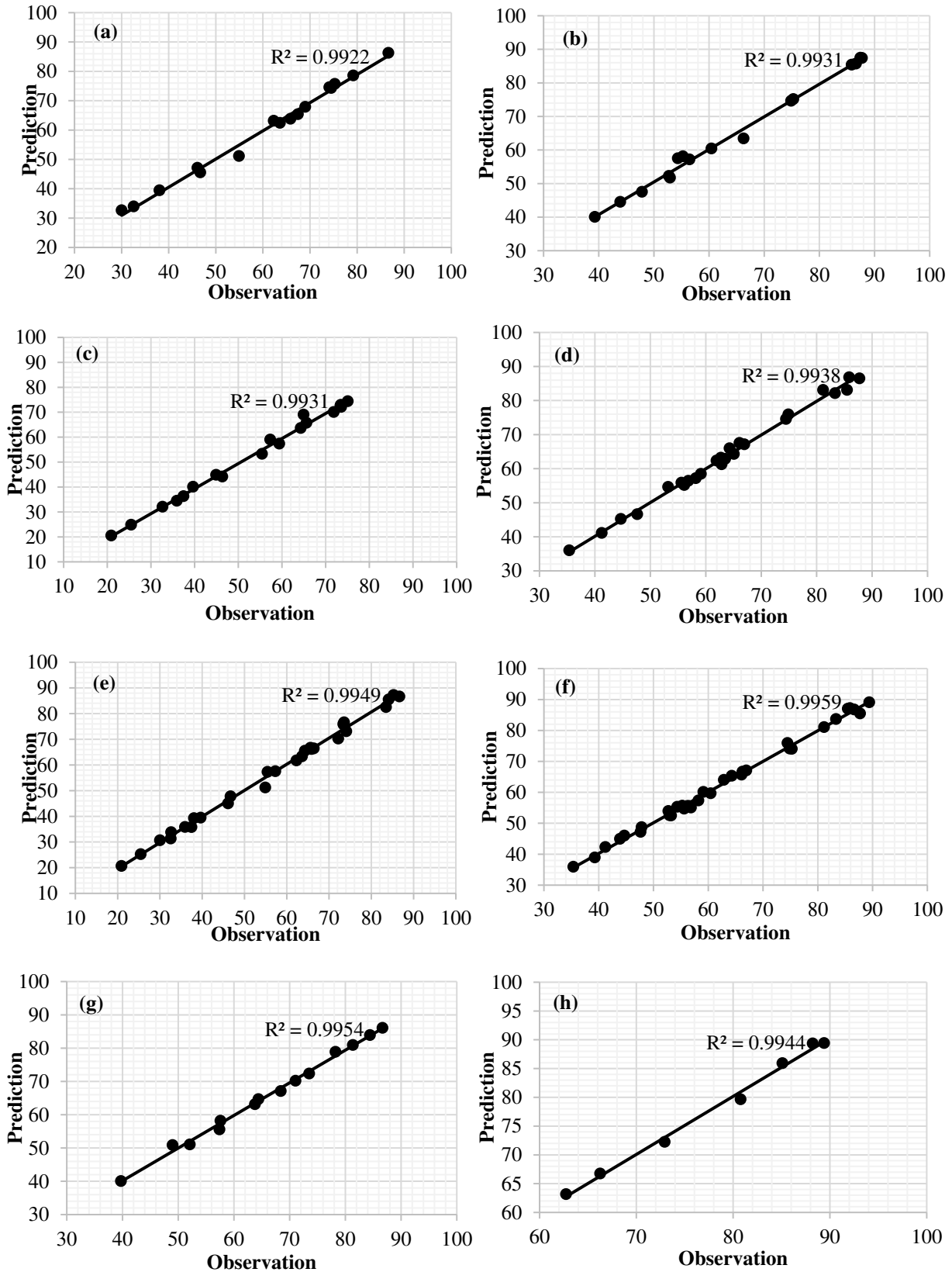
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346 **Table 6.** The results of the regression analysis for SMN-PSO predictions

| Exp. No | Process | # Samples | $Y = \hat{\beta}Y_{pre}$ | 95% Confidence Interval of β | | $R^2(\%)$ |
|---------|--------------------------|-----------|--------------------------|------------------------------------|-------------|-----------|
| | | | | Lower Bound | Upper Bound | |
| 1 | Classical-Fenton Process | 16 | $Y = 1.006850Y_{pre}$ | 0.993262 | 1.020438 | 99.9399 |
| 2 | Photo-Fenton Process | 16 | $Y = 1.0002654Y_{pre}$ | 0.988809 | 1.011720 | 99.9567 |
| 3 | Classical-Fenton Process | 19 | $Y = 1.008765Y_{pre}$ | 0.995706 | 1.021824 | 99.9317 |
| 4 | Photo-Fenton Process | 25 | $Y = 1.001056Y_{pre}$ | 0.994011 | 1.008101 | 99.9721 |
| 5 | Classical-Fenton Process | 29 | $Y = 0.994154Y_{pre}$ | 0.985077 | 1.003231 | 99.9444 |
| 6 | Photo-Fenton Process | 35 | $Y = 0.999413Y_{pre}$ | 0.994233 | 1.004593 | 99.9779 |
| 7 | Classical-Fenton Process | 14 | $Y = 1.005520Y_{pre}$ | 0.997223 | 1.013818 | 99.9810 |
| 8 | Photo-Fenton Process | 7 | $Y = 0.997960Y_{pre}$ | 0.988405 | 1.007515 | 99.9908 |

347

348 The findings given in Table 4 can be investigated from three different angles. For all
 349 experiments, the beta coefficient estimates obtained in the regression estimation equation are
 350 pretty close to 1 as expected for a successful prediction tool, a sign that the predictions
 351 produced by SMN-PSO are very close to the actual observations. Moreover, the confidence
 352 intervals of β (with 95% probability) coefficients cover 1 and also had a very narrow frame. In
 353 other words, it can be said that beta coefficients are equal to 1 with a probability of 95%. In
 354 addition, the fact that the determination coefficient, R^2 , is very close to 1 for each experiment
 355 can be seen as proof of the existence of a very high linear relationship between the predictions
 356 of SMN-PSO and the actual removal values. This is another feature that a superior prediction
 357 tool should have, just like the SMN-PSO.



358 **Fig. 4.** The scatter gram of observed and predicted removals (a: Exp.1; b: Exp. 2; c: Exp. 3;
 359 d: Exp. 4; e: Exp. 5; f: Exp. 6; g: Exp. 7; h: Exp. 8)

360 Moreover, besides all these statistical evaluations, scatter diagrams displaying the
 361 observed and predicted removal efficiency values were used to visualize the superior

362 prediction performance of the SMN-PSO as the best of the NN-based models used in this
 363 study. In a scatter plot, for a prediction tool which is produced satisfactory predictions, it is
 364 expected that most of the points on the scatter plots are in proximity to the line segment. The
 365 scatter plots, given in Figure 4, also contain examples of exactly this situation. In other words,
 366 in the scatter plots, the points were spread very close to the line.

367

368 3.4. Optimization via genetic algorithm

369 After the modelling process, as the final goal of the study, the various operating
 370 conditions used for the analysis process were optimized. For this purpose, GA was used to
 371 optimize the independent variables to maximize the removal efficiency rate. Here, the basic
 372 principle is to determine the independent variable values that will maximize the efficiency of
 373 the removal. Generally, the objective function intended to be maximized is given as in Eq.
 374 (12).

$$y = f(X_1, X_2) \quad (12)$$

375

376 where y is the removal performance of Classical and Photo-Fenton Processes from
 377 cosmetic wastewater, X_1 and X_2 represent the independent variables such as H_2O_2 doses,
 378 Fe(II) doses, and $H_2O_2/Fe(II)$ rates. The optimization process was carried out for only the
 379 SMN-PSO, which showed the highest prediction performance among the three NN-based
 380 prediction models used in this study. In this case, the objective function can be given as
 381 follows:

$$y = f\left(\frac{1}{1 + e^{-((X_1 \times w_1 + b_1) \times (X_2 \times w_2 + b_2))}}\right) \quad (12)$$

382

383 The basic framework of the optimization process for each experiment is summarized in
 384 Table 7. An important advantage in modelling this type of data by using NN is that yields of
 385 removal corresponding to non-existent parameter values in performed experiments can also be
 386 revealed. Moreover, by using the fitness function of a trained neural network, an optimization
 387 process performed through GA can determine the optimum values of the experimental
 388 parameters to maximize efficiency. Furthermore, it is possible that these values differ from
 389 the parameter values used in the experiments already performed. From this perspective, using
 390 the fitness function from the SMN-PSO, the parameters of the experiments were optimized
 391 via GA. Thus, without the need for many different experiments, the optimum parameter
 392 values can be determined to get the maximum removal ratios. When the results given in Table
 393 5 are exemplified; for Experiment 1, with Fe(II) dosage 399.999 mg/L and H_2O_2 dosage
 394 726.1816 mg/L, the optimized condition leads to maximum removal performance (86.4965%)
 395 with 99.70% desirability.

396 The results of the optimization transaction can be also used to comparatively evaluate the
 397 performance of Classical and Photo-Fenton processes. From these results, under the optimum
 398 conditions, it is clearly seen that Photo-Fenton processes have higher COD removal
 399 performance from cosmetic wastewater in each experiment.

400

401 **Table 7.** The framework of the optimization process

| Exp. No | Process | Constraints | Optimal Values | Objective Function Values | Desirability |
|---------|------------------|---------------------------------------|----------------|---------------------------|--------------|
| 1 | Classical-Fenton | $50 \leq Fe(II) (mg/L) \leq 400$ | 399.9999 | 86.4965 | 99.70% |
| | | $600 \leq H2O2(mg/L) \leq 900$ | 726.1686 | | |
| 2 | Photo-Fenton | $50 \leq Fe(II) mg/L \leq 400$ | 399.9998 | 87.4862 | 99.48% |
| | | $600 \leq H2O2(mg/L) \leq 900$ | 894.0719 | | |
| 3 | Classical-Fenton | $200 \leq H2O2(mg/L) \leq 1050$ | 992.0797 | 75.0394 | 99.90% |
| | | $150 \leq Fe(II)(mg/L) \leq 400$ | 350.3543 | | |
| 4 | Photo-Fenton | $200 \leq H2O2(mg/L) \leq 1050$ | 1029.1429 | 87.4848 | 99.52% |
| | | $150 \leq Fe(II)(mg/L) \leq 400$ | 399.9869 | | |
| 5 | Classical-Fenton | $200 \leq H2O2(mg/L) \leq 1050$ | 951.9432 | 86.6637 | 100.00% |
| | | $50 \leq Fe(II) (mg/L) \leq 400$ | 400 | | |
| 6 | Photo-Fenton | $200 \leq H2O2(mg/L) \leq 1050$ | 992.0543 | 89.2568 | 99.71% |
| | | $50 \leq Fe(II) (mg/L) \leq 400$ | 399.9994 | | |
| 7 | Classical-Fenton | $0 \leq Contact\ time\ (min) \leq 60$ | 60 | 86.6868 | 99.99% |
| | | $150 \leq Fe(II)(mg/L) \leq 400$ | 335.3312 | | |
| 8 | Photo-Fenton | $0 \leq Contact\ time\ (min) \leq 60$ | 60 | 89.4118 | 100.00% |
| | | $Fe(II)(mg/L) = 300$ | 300 | | |

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404 *3.5. Comparison of the results*

405 When the results obtained from each model were examined in detail, it was observed that
 406 NN-models produced much better prediction results than RSM. The averages of success
 407 rankings created by taking into account the performance of all models for eight different
 408 experiments, according to RMSE and MAPE criteria, also support this situation. Considering
 409 the averages of success rankings, as can be clearly seen in Figures 5-6, SMN-PSO had much
 410 better performance than other NN-based models for training, validation, and test sets.
 411 Moreover, when all data sets were considered, it was also observed that SMN-PSO had a
 412 superior prediction performance than both other NN-based models and RSM.

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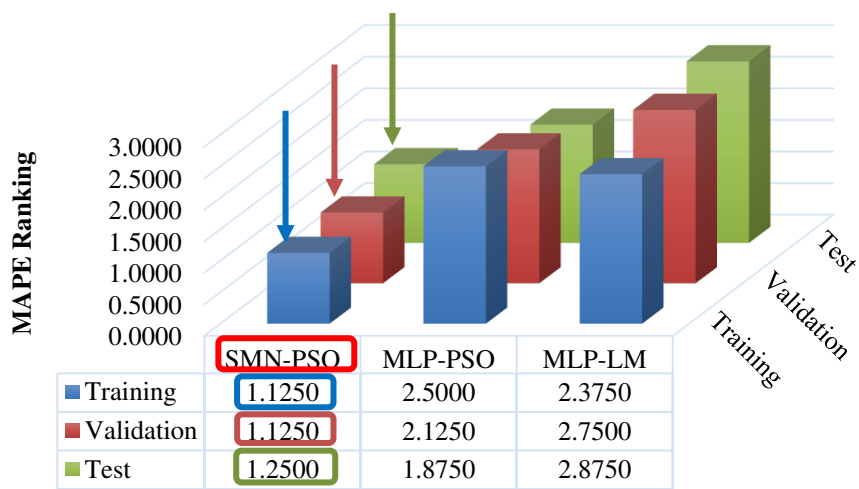
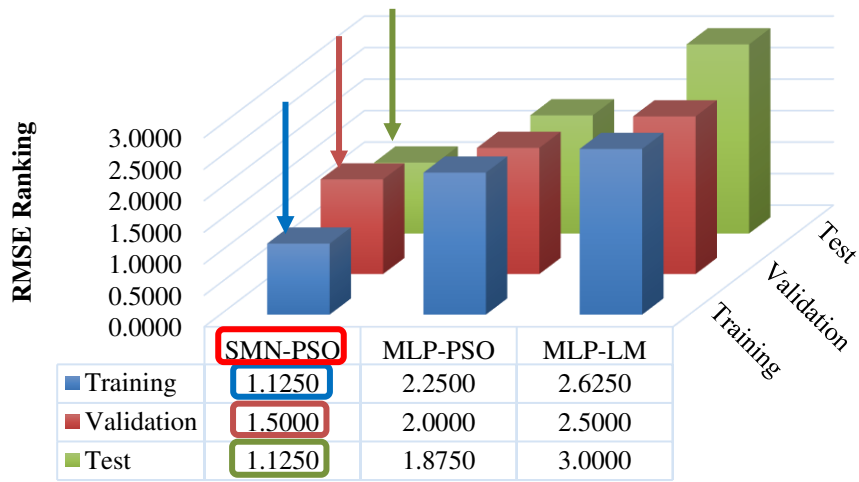
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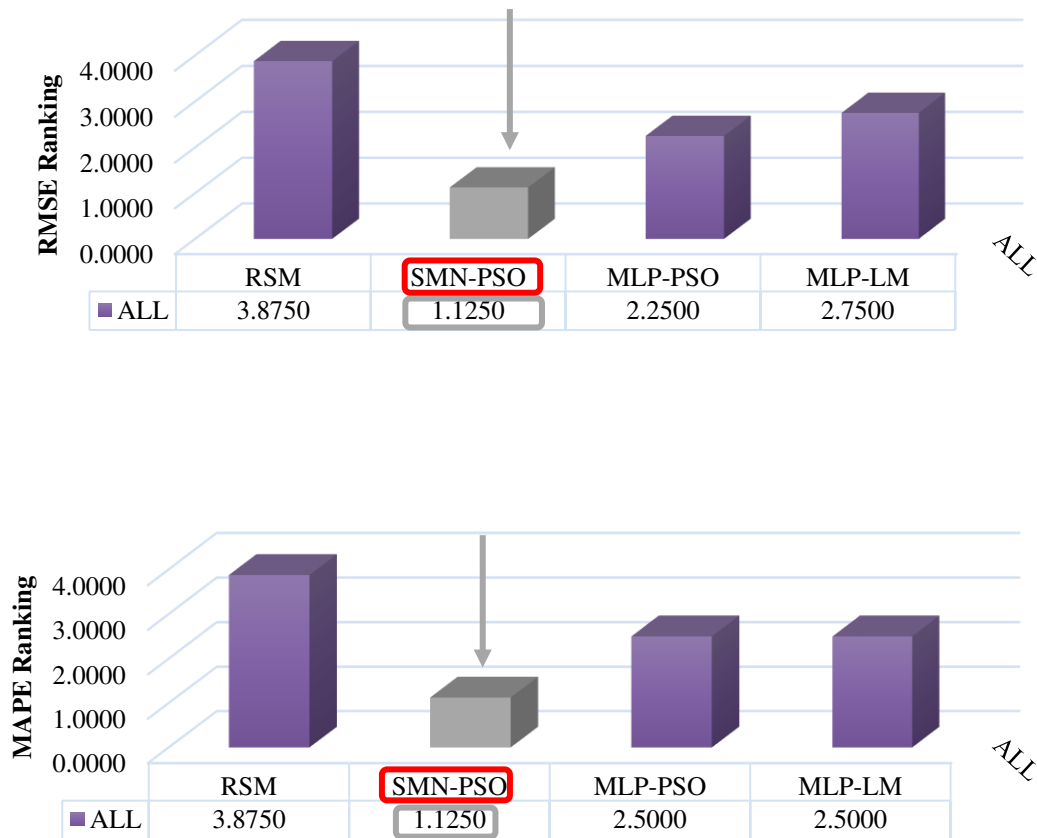
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421 **Fig. 5.** Comparing NN-based models in terms of RMSE and MAPE

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425 **Fig. 6.** Comparing all models in terms of RMSE and MAPE

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427 **4. Conclusion**

428 In this study, the prediction of COD removal performance of Classical and Photo-Fenton
 429 Processes from cosmetic wastewater was performed by using statistics-based RSM and NN-
 430 based three machine learning models. Among all methods, SMN-PSO was observed to be the
 431 model that produces the best predictive results in almost all cases.

- 432 • While SMN-PSO mostly produced predictions with an RMSE value of around 1%, in
 433 many cases, it was observed that this value was even below 1%.
- 434 • In terms of the MAPE criterion, which is a measure of the percentage error, SMN-
 435 PSO revealed errors of less than 1% and 2% in most cases and even less than 1% in
 436 some cases.
- 437 • Considering the average of the success rankings, it can be clearly seen that the SMN-
 438 PSO produces far superior prediction results compared to other models in terms of
 439 both criteria.
- 440 • The SMN-PSO, which has the best predictive performance in almost all situations,
 441 also performed satisfactorily and competitively in other situations.

442 There are several main reasons why SMN-PSO exhibits superior prediction success;

- 443 • Since the SMN-PSO is trained by PSO, it does not get caught in local optimum traps
444 unlike derivative-based training algorithms such as LM.
- 445 • With the multiplicative aggregation function, SMN-PSO has a higher ability to the
446 adaptation to nonlinear problems.
- 447 • Moreover, SMN-PSO, unlike MLPs, does not include a problem such as determining
448 the architecture.

449 Another unique aspect of this study is that the independent variables are optimized by a
450 genetic algorithm for SMN-PSO, which is used as a function approximation and produces the
451 best prediction results. Here, using the genetic algorithm, the independent values to maximize
452 COD removal performance are obtained in a particular search field. COD removal
453 performances corresponding to the obtained optimum independent variable values provided
454 high desirability values. Moreover, by this means, it is not necessary to perform an additional
455 experiment to achieve all these.

456 With this study, the optimum conditions can be determined more accurately by modeling
457 the findings obtained from the limited number of experiments conducted to determine the
458 performance of the treatment processes. In this way, technical difficulties, costs, manpower,
459 and time are no longer a problem, and the estimates of the models trained with the available
460 data allow the process to work efficiently. In future studies, statistical-based prediction
461 models and NN-based machine learning models can be combined to get better predictions of
462 removal performance.

463
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465 **References**

- 466 Baird RB, Eaton AD, Rice EW (2017) Standard Methods for the Examination of Water and
467 Wastewater. 23rd edition
- 468 Banerjee P, Dey T kumar, Sarkar S, et al (2016) Treatment of cosmetic effluent in different
469 configurations of ceramic UF membrane based bioreactor: Toxicity evaluation of the
470 untreated and treated wastewater using catfish (*Heteropneustes fossilis*). *Chemosphere*
471 146:133–144. <https://doi.org/10.1016/j.chemosphere.2015.12.004>
- 472 Baştürk E, Alver A (2019) Modeling azo dye removal by sono-fenton processes using
473 response surface methodology and artificial neural network approaches. *J Environ*
474 *Manage* 248:109300
- 475 Bautista P, Mohedano AF, Gilarranz MA, et al (2007) Application of Fenton oxidation to
476 cosmetic wastewaters treatment. *J Hazard Mater* 143:128–134.
477 <https://doi.org/10.1016/j.jhazmat.2006.09.004>
- 478 Bautista P, Mohedano AF, Menéndez N, et al (2010) Catalytic wet peroxide oxidation of
479 cosmetic wastewaters with Fe-bearing catalysts. *Catal Today* 151:148–152.
480 <https://doi.org/10.1016/j.cattod.2010.01.023>
- 481 Bom S, Jorge J, Ribeiro HM, Marto J (2019) A step forward on sustainability in the cosmetics
482 industry: A review. *J Clean Prod* 225:270–290.
483 <https://doi.org/10.1016/j.jclepro.2019.03.255>
- 484 Cagcag Yolcu O, Bas E, Egrioglu E, Yolcu U (2018) Single Multiplicative Neuron Model

485 Artificial Neural Network with Autoregressive Coefficient for Time Series Modelling.
486 *Neural Process Lett* 47:1133–1147. <https://doi.org/10.1007/s11063-017-9686-3>

487 de Andrade PM, Dufrayer CR, Ionashiro EY, de Brito NN (2020) The use of metallurgical
488 waste for heterogeneous photo Fenton-Like treatment of cosmetic effluent. *J Environ*
489 *Chem Eng* 8:104148. <https://doi.org/10.1016/j.jece.2020.104148>

490 Egrioglu E, Aladag C, Yolcu U, et al (2013) Fuzzy Time Series Method Based on
491 Multiplicative Neuron Model and Membership Values. *Am J Intell Syst* 3:33–39.
492 <https://doi.org/10.5923/j.ajis.20130301.05>

493 El-Gohary F, Tawfik A, Mahmoud U (2010) Comparative study between chemical
494 coagulation/precipitation (C/P) versus coagulation/dissolved air flotation (C/DAF) for
495 pre-treatment of personal care products (PCPs) wastewater. *Desalination* 252:106–112.
496 <https://doi.org/10.1016/j.desal.2009.10.016>

497 Elmolla ES, Chaudhuri M, Eltoukhy MM (2010) The use of artificial neural network (ANN)
498 for modeling of COD removal from antibiotic aqueous solution by the Fenton process. *J*
499 *Hazard Mater* 179:127–134. <https://doi.org/10.1016/j.jhazmat.2010.02.068>

500 Fernandes NC, Brito LB, Costa GG, et al (2018) Removal of azo dye using Fenton and
501 Fenton-like processes: Evaluation of process factors by Box–Behnken design and
502 ecotoxicity tests. *Chem Biol Interact* 291:47–54

503 Friha I, Karray F, Feki F, et al (2014) Treatment of cosmetic industry wastewater by
504 submerged membrane bioreactor with consideration of microbial community dynamics.
505 *Int Biodeterior Biodegrad* 88:125–133. <https://doi.org/10.1016/j.ibiod.2013.12.015>

506 Gholizadeh AM, Zarei M, Ebratkhan M, Hasanzadeh A (2021) Phenazopyridine
507 degradation by electro-Fenton process with magnetite nanoparticles-activated carbon
508 cathode, artificial neural networks modeling. *J Environ Chem Eng* 9:104999.
509 <https://doi.org/10.1016/j.jece.2020.104999>

510 Goldberg DE (1989) *Genetic Algorithms in Search, Optimization and Machine Learning* 13th
511 ed. Edition. Addison-Wesley Publishing Company, Boston, United States

512 Haykin S (1999) *Neural Networks: A Comprehensive Foundation*, 2nd edn. Prentice-Hall,
513 New York

514 Holland JH (1992) *Adaptation in Natural and Artificial Systems: An Introductory Analysis*
515 with Applications to Biology, Control, and Artificial Intelligence. MIT Press

516 Jaafarzadeh N, Ahmadi M, Amiri H, et al (2012) Predicting Fenton modification of solid
517 waste vegetable oil industry for arsenic removal using artificial neural networks. *J*
518 *Taiwan Inst Chem Eng* 43:873–878. <https://doi.org/10.1016/j.jtice.2012.05.008>

519 Kennedy J, Eberhart R (1995) Particle Swarm Optimisation. In: *Proceedings of IEEE*
520 *international conference on neural networks*. Piscataway, NJ: IEEE Service Center,
521 Perth, Australia, pp 1942–1948

522 Lek S, Delacoste M, Baran P, et al (1996) Application of neural networks to modelling
523 nonlinear relationships in ecology. *Ecol Modell* 90:39–52. [https://doi.org/10.1016/0304-](https://doi.org/10.1016/0304-3800(95)00142-5)
524 [3800\(95\)00142-5](https://doi.org/10.1016/0304-3800(95)00142-5)

- 525 Li D, Lv R, Si G, You Y (2017) Hybrid neural network-based prediction model for
526 tribological properties of polyamide6-based friction materials. *Polym Compos* 38:1705–
527 1711
- 528 Ma Y, Jiang C, Hou Z, Wang C (2006) The formulation of the optimal strategies for the
529 electricity producers based on the particle swarm optimization algorithm. *IEEE Trans*
530 *Power Syst* 21:1663–1671. <https://doi.org/10.1109/TPWRS.2006.883676>
- 531 Melo ED de, Mounteer AH, Leão LH de S, et al (2013) Toxicity identification evaluation of
532 cosmetics industry wastewater. *J Hazard Mater* 244–245:329–334.
533 <https://doi.org/10.1016/j.jhazmat.2012.11.051>
- 534 Monsalvo VM, Lopez J, Mohedano AF, Rodriguez JJ (2014) Treatment of cosmetic
535 wastewater by a full-scale membrane bioreactor (MBR). *Environ Sci Pollut Res*
536 21:12662–12670. <https://doi.org/10.1007/s11356-014-3208-x>
- 537 Muszyński A, Marcinowski P, Maksymiec J, et al (2019) Cosmetic wastewater treatment with
538 combined light/Fe⁰/H₂O₂ process coupled with activated sludge. *J Hazard Mater*
539 378:120732. <https://doi.org/10.1016/j.jhazmat.2019.06.009>
- 540 Naumczyk J, Bogacki J, Marcinowski P, Kowalik P (2014) Cosmetic wastewater treatment by
541 coagulation and advanced oxidation processes. *Environ Technol (United Kingdom)*
542 35:541–548. <https://doi.org/10.1080/09593330.2013.808245>
- 543 Oller I, Malato S, Sánchez-Pérez JA (2011) Combination of Advanced Oxidation Processes
544 and biological treatments for wastewater decontamination-A review. *Sci Total Environ*
545 409:4141–4166. <https://doi.org/10.1016/j.scitotenv.2010.08.061>
- 546 Paździor K, Bilińska L, Ledakowicz S (2019) A review of the existing and emerging
547 technologies in the combination of AOPs and biological processes in industrial textile
548 wastewater treatment. *Chem Eng J* 376:120597.
549 <https://doi.org/10.1016/j.cej.2018.12.057>
- 550 Puyol D, Monsalvo VM, Mohedano AF, et al (2011) Cosmetic wastewater treatment by
551 upflow anaerobic sludge blanket reactor. *J Hazard Mater* 185:1059–1065.
552 <https://doi.org/10.1016/j.jhazmat.2010.10.014>
- 553 Radwan M, Gar Alalm M, Eletriby H (2018) Optimization and modeling of electro-Fenton
554 process for treatment of phenolic wastewater using nickel and sacrificial stainless steel
555 anodes. *J Water Process Eng* 22:155–162. <https://doi.org/10.1016/j.jwpe.2018.02.003>
- 556 Rumelhart E, Hinton G, Williams R (1986) Learning internal representations by error
557 propagation. *The M.I.T. Press, Cambridge*, pp 318–362
- 558 Sabour MR, Amiri A (2017) Comparative study of ANN and RSM for simultaneous
559 optimization of multiple targets in Fenton treatment of landfill leachate. *Waste Manag*
560 65:54–62. <https://doi.org/10.1016/j.wasman.2017.03.048>
- 561 Shi Y, Eberhart RC (1999) Empirical study of particle swarm optimization. *Proc 1999 Congr*
562 *Evol Comput CEC 1999* 3:1945–1950. <https://doi.org/10.1109/CEC.1999.785511>
- 563 Talwar S, Verma AK, Sangal VK (2019) Modeling and optimization of fixed mode dual
564 effect (photocatalysis and photo-Fenton) assisted Metronidazole degradation using ANN
565 coupled with genetic algorithm. *J Environ Manage* 250:.

566 <https://doi.org/10.1016/j.jenvman.2019.109428>

567 Tolba A, Gar Alalm M, Elsamadony M, et al (2019) Modeling and optimization of
568 heterogeneous Fenton-like and photo-Fenton processes using reusable Fe₃O₄-
569 MWCNTs. *Process Saf Environ Prot* 128:273–283.
570 <https://doi.org/10.1016/j.psep.2019.06.011>

571 Werbos P (1974) *Beyond Regression: New Tools for Prediction and Analysis in the*
572 *Behavioral Sciences*. Harvard University

573 Wiliński PR, Marcinowski PP, Naumczyk J, Bogacki J (2017) Pretreatment of cosmetic
574 wastewater by dissolved ozone flotation (DOF). *Desalin Water Treat* 71:95–106.
575 <https://doi.org/10.5004/dwt.2017.20552>

576 Yadav RN, Kalra PK, John J (2007) Time series prediction with single multiplicative neuron
577 model. *Appl Soft Comput J* 7:1157–1163. <https://doi.org/10.1016/j.asoc.2006.01.003>

578 Yolcu U, Egrioglu E, Bas E, et al (2019) Probabilistic forecasting, linearity and nonlinearity
579 hypothesis tests with bootstrapped linear and nonlinear artificial neural network. *J Exp*
580 *Theor Artif Intell* 00:1–22. <https://doi.org/10.1080/0952813X.2019.1595167>

581 Zarei M, Khataee AR, Ordikhani-Seyedlar R, Fathinia M (2010) Photoelectro-Fenton
582 combined with photocatalytic process for degradation of an azo dye using supported
583 TiO₂ nanoparticles and carbon nanotube cathode: Neural network modeling.
584 *Electrochim Acta* 55:7259–7265. <https://doi.org/10.1016/j.electacta.2010.07.050>

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610 **FAT:** Supervision, Data curation, Writing- Original draft preparation, Visualization,
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Figures



Figure 1

A schematic representation of Photo-Fenton Process

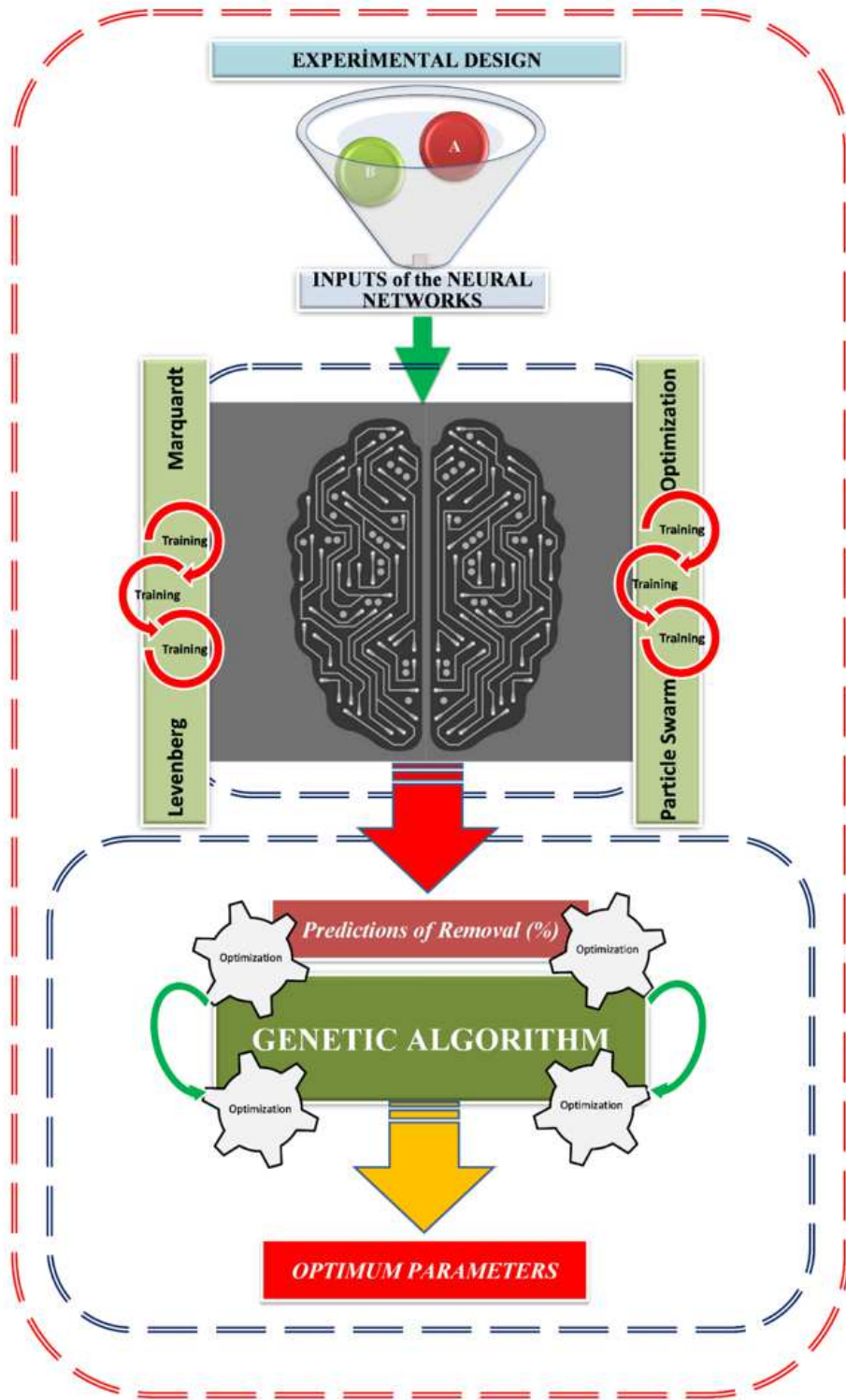


Figure 2

A scheme of the combination of ANNs and heuristic algorithms

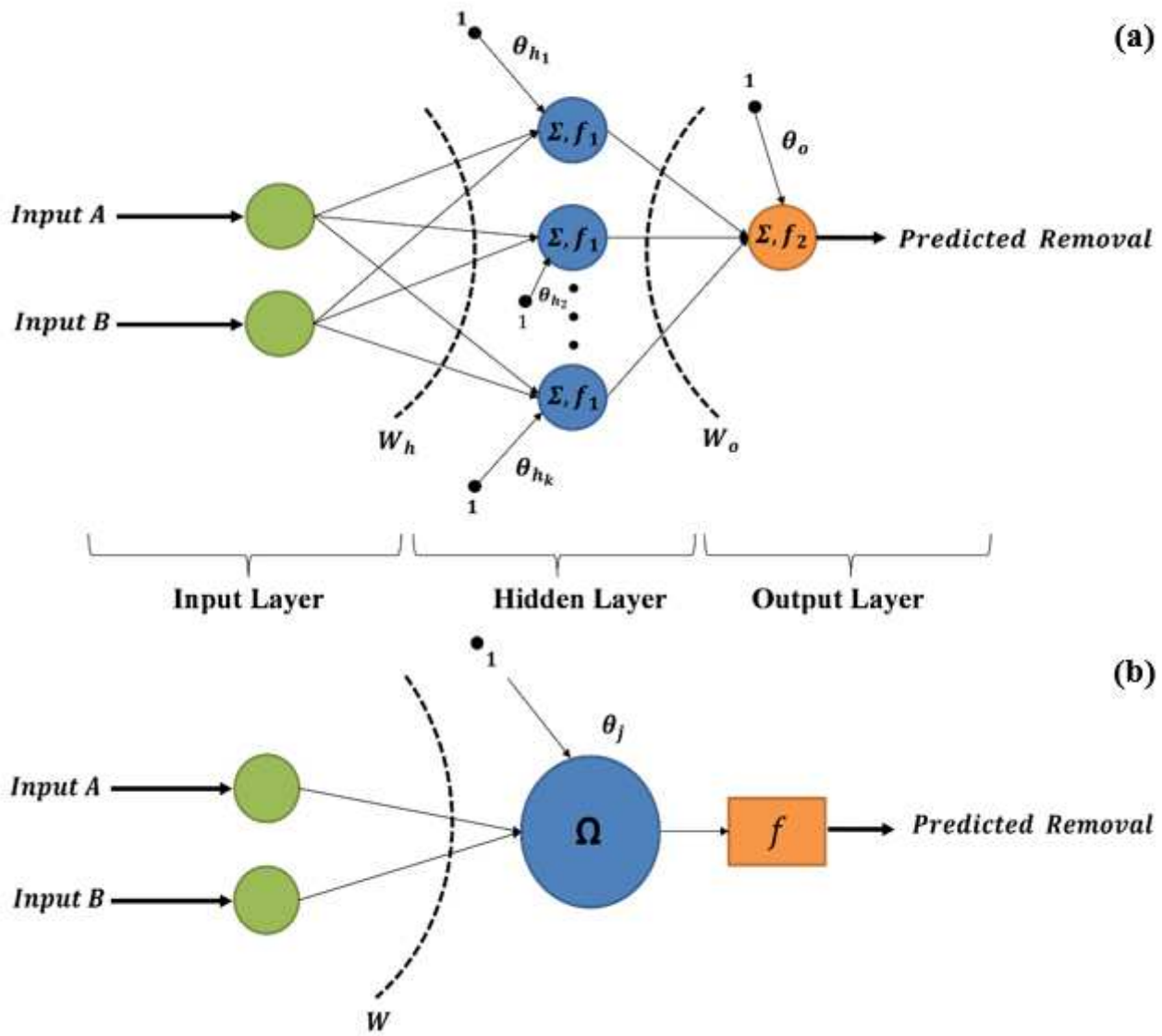


Figure 3

An illustration of MLP structure / 2-k-1 Architecture (a) and SMN structure (b)

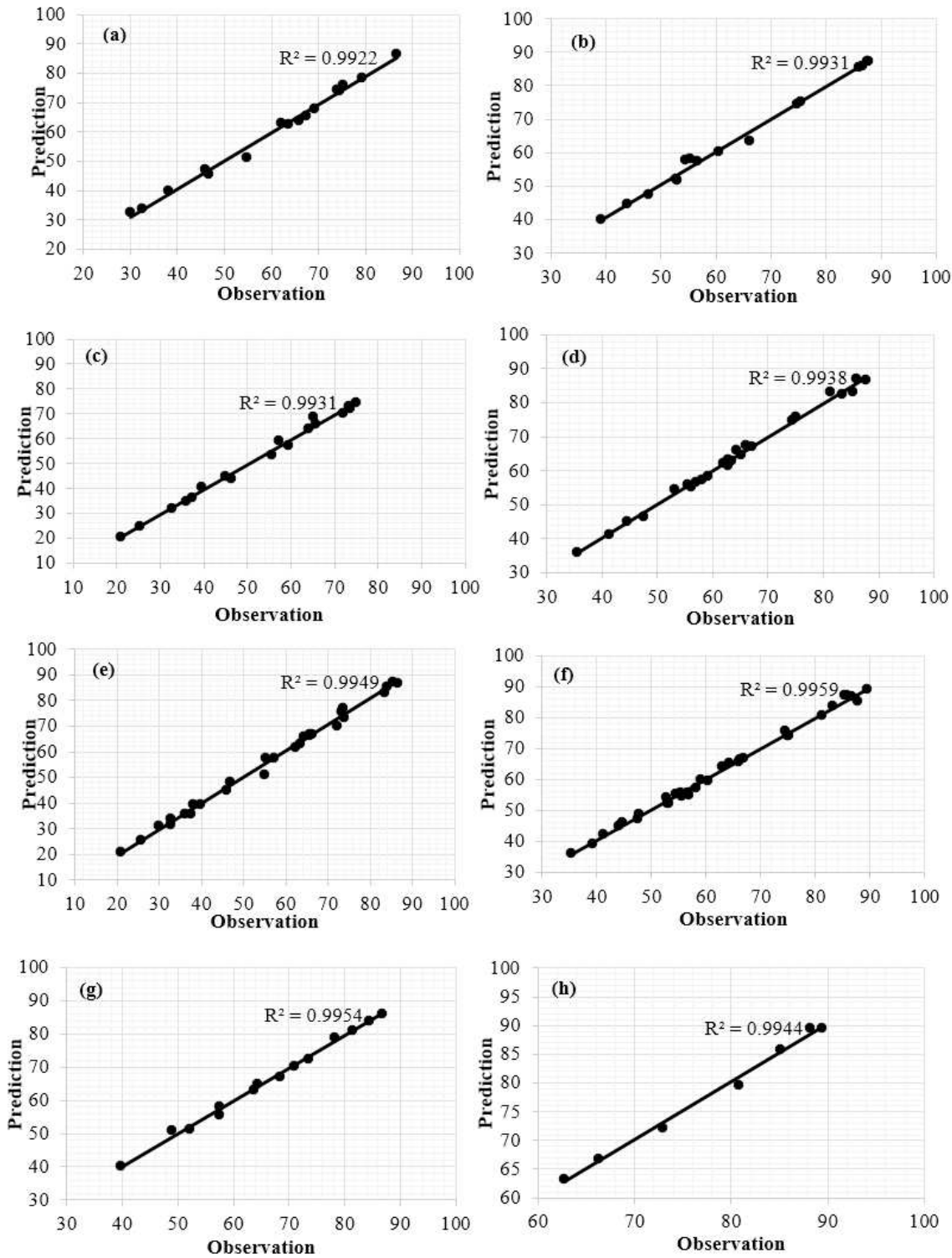


Figure 4

The scatter gram of observed and predicted removals (a: Exp.1; b: Exp. 2; c: Exp. 3; d: Exp. 4; e: Exp. 5; f: Exp. 6; g: Exp. 7; h: Exp. 8)

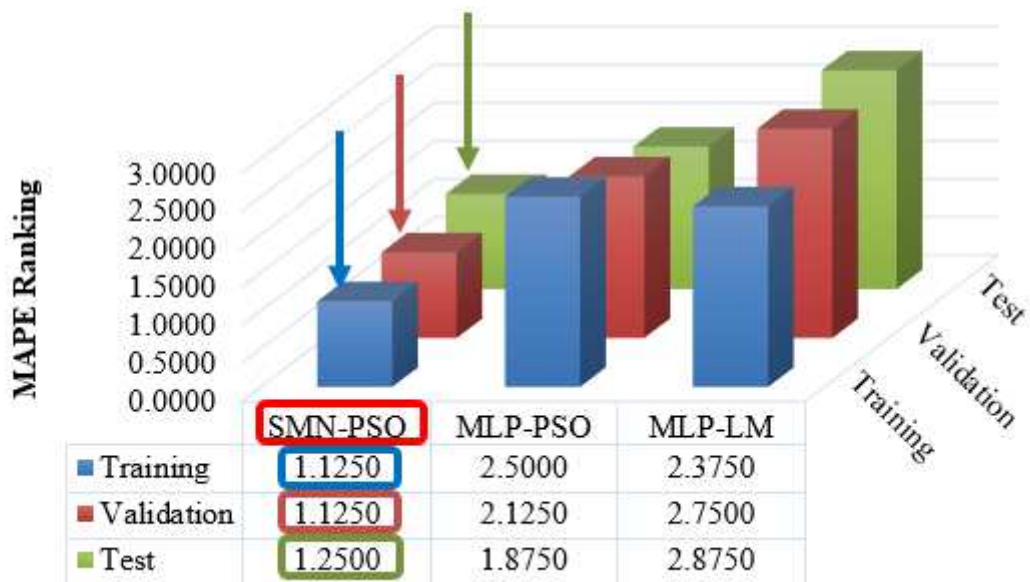
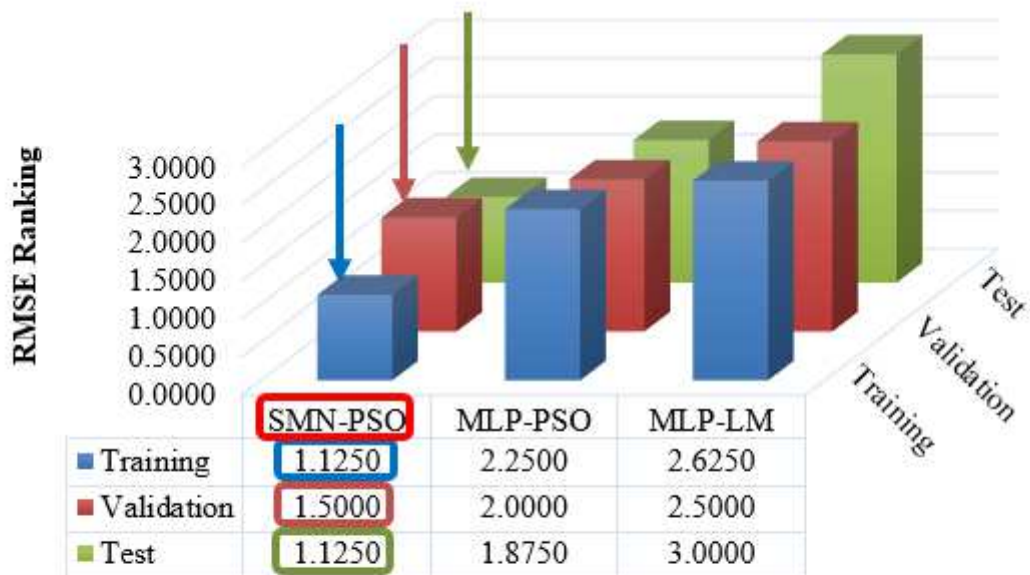


Figure 5

Comparing NN-based models in terms of RMSE and MAPE

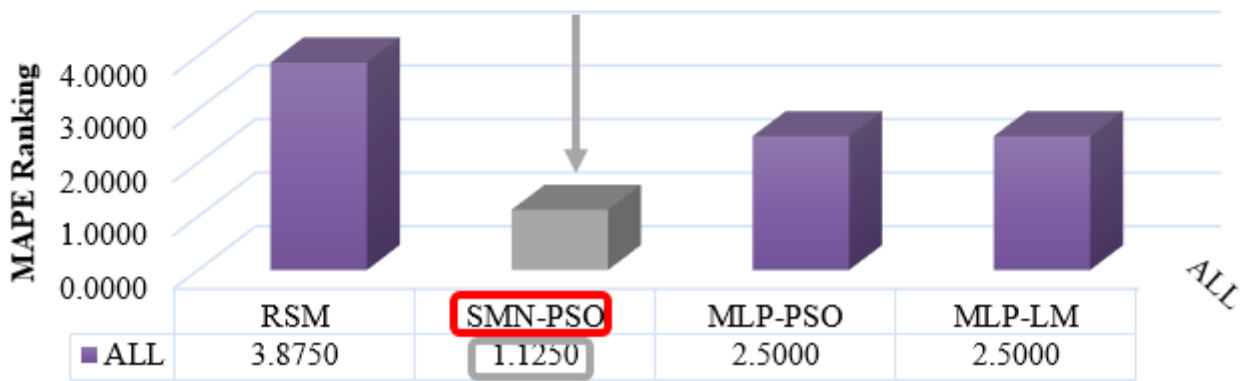
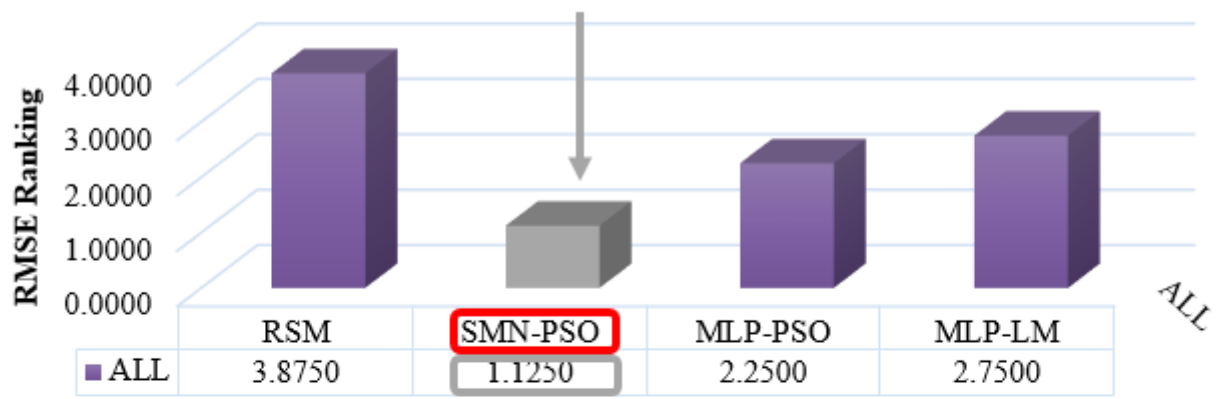


Figure 6

Comparing all models in terms of RMSE and MAPE