



Running of the top quark mass from proton-proton collisions at $\sqrt{s} = 13$ TeV

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ABSTRACT

The running of the top quark mass is experimentally investigated for the first time. The mass of the top quark in the modified minimal subtraction ($\overline{\text{MS}}$) renormalization scheme is extracted from a comparison of the differential top quark-antiquark ($t\bar{t}$) cross section as a function of the invariant mass of the $t\bar{t}$ system to next-to-leading-order theoretical predictions. The differential cross section is determined at the parton level by means of a maximum-likelihood fit to distributions of final-state observables. The analysis is performed using $t\bar{t}$ candidate events in the $e^{\pm}\mu^{\mp}$ channel in proton-proton collision data at a centre-of-mass energy of 13 TeV recorded by the CMS detector at the CERN LHC in 2016, corresponding to an integrated luminosity of 35.9 fb^{-1} . The extracted running is found to be compatible with the scale dependence predicted by the corresponding renormalization group equation. In this analysis, the running is probed up to a scale of the order of 1 TeV.

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1. Introduction

Beyond leading order in perturbation theory, the fundamental parameters of the quantum chromodynamics (QCD) Lagrangian, i.e. the strong coupling constant α_S and the quark masses, are subject to renormalization. As a result, these parameters depend on the scale at which they are evaluated. The evolution of α_S and of the quark masses as a function of the scale, commonly referred to as “running”, is described by renormalization group equations (RGEs). The running of α_S was experimentally verified on a wide range of scales using jet production in electron-proton, positron-proton, electron-positron, proton-antiproton, and proton-proton (pp) collisions, as summarized, e.g. in Refs. [1,2]. To determine the running, the value of α_S evaluated at an arbitrary reference scale is extracted in bins of a physical energy scale Q and then converted to $\alpha_S(Q)$ using the corresponding RGE [2]. The validity of this procedure lies in the fact that, in a calculation, the renormalization scale is normally identified with the physical energy scale of the process. The same procedure can be used to determine the running of the mass of a quark. In the modified minimal subtraction ($\overline{\text{MS}}$) renormalization scheme, the dependence of a quark mass m on the scale μ is described by the RGE

$$\mu^2 \frac{dm(\mu)}{d\mu^2} = -\gamma(\alpha_S(\mu)) m(\mu), \quad (1)$$

where $\gamma(\alpha_S(\mu))$ is the mass anomalous dimension, which is known up to five-loop order in perturbative QCD [3,4]. The solution of Eq. (1) can be used to obtain the quark mass at any scale μ from the mass evaluated at an initial scale μ_0 . The running of the b quark mass was demonstrated [5] using data from various experiments at the CERN LEP [6–9], SLAC SLC [10], and DESY HERA [11] colliders. Measurements of charm quark pair production in deep inelastic scattering at the DESY HERA were used to determine the running of the charm quark mass [12]. These measurements represent a powerful test of the validity of perturbative QCD. Furthermore, RGEs can be modified by contributions from physics beyond the standard model, e.g. in the context of supersymmetric theories [13].

This Letter describes the first experimental investigation of the running of the top quark mass, m_t , as defined in the $\overline{\text{MS}}$ scheme. The running of m_t is extracted from a measurement of the differential top quark-antiquark pair production cross section, $\sigma_{t\bar{t}}$, as a function of the invariant mass of the $t\bar{t}$ system, $m_{t\bar{t}}$. The differential cross section, $d\sigma_{t\bar{t}}/dm_{t\bar{t}}$, is determined at the parton level by means of a maximum-likelihood fit to distributions of final-state observables using $t\bar{t}$ candidate events in the $e^{\pm}\mu^{\mp}$ final state, extending the method described in Ref. [14] to the case of a differential measurement. This method allows the differential cross section to be constrained simultaneously with the systematic uncertain-

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ties. In this analysis, the parton level is defined before radiation from the parton shower, which allows for a direct comparison with fixed-order theoretical predictions. The measurement is performed using pp collision data at $\sqrt{s} = 13$ TeV recorded by the CMS detector at the CERN LHC in 2016, corresponding to an integrated luminosity of 35.9 fb^{-1} . The running mass, $m_t(\mu)$, is extracted at next-to-leading order (NLO) in QCD as a function of $m_{t\bar{t}}$ by comparing fixed-order theoretical predictions at NLO to the measured $d\sigma_{t\bar{t}}/dm_{t\bar{t}}$. The running of m_t is probed up to a scale of the order of 1 TeV.

2. The CMS detector and Monte Carlo simulation

The central feature of the CMS apparatus is a superconducting solenoid of 6 m internal diameter, providing a magnetic field of 3.8 T. Within the solenoid volume are a silicon pixel and strip tracker, a lead tungstate crystal electromagnetic calorimeter (ECAL), and a brass and scintillator hadron calorimeter, each composed of a barrel and two endcap sections. Forward calorimeters extend the pseudorapidity (η) coverage provided by the barrel and endcap detectors. Muons are detected in gas-ionization chambers embedded in the steel flux-return yoke outside the solenoid. A two-level trigger system selects events of interest for analysis [15]. A more detailed description of the CMS detector, together with a definition of the coordinate system used and the relevant kinematic variables, can be found in Ref. [16].

The particle-flow (PF) algorithm [17] aims to reconstruct and identify electrons, muons, photons, charged and neutral hadrons in an event, with an optimized combination of information from the various elements of the CMS detector. The energy of electrons is determined from a combination of the electron momentum at the primary interaction vertex as determined by the tracker, the energy of the corresponding ECAL cluster, and the energy sum of all bremsstrahlung photons spatially compatible with originating from the electron track [18]. The momentum of muons is obtained from the curvature of the corresponding track [19]. Jets are reconstructed from the PF candidates using the anti- k_T clustering algorithm with a distance parameter of 0.4 [20,21], and the jet momentum is determined as the vectorial sum of all particle momenta in the jet. The missing transverse momentum vector is computed as the negative vector sum of the transverse momenta (p_T) of all the PF candidates in an event. Jets originating from the hadronization of b quarks (b jets) are identified (b tagged) using the combined secondary vertex [22] algorithm, using a working point that corresponds to an average b tagging efficiency of 41% for simulated $t\bar{t}$ events, and an average misidentification probability of 0.1% and 2.2% for light-flavour jets and c jets, respectively [22].

In this analysis, the same Monte Carlo (MC) simulations as in Ref. [14] are used. In particular, $t\bar{t}$, tW , and Drell–Yan (DY) events are simulated using the POWHEG v2 [23–28] NLO MC generator interfaced to PYTHIA 8.202 [29] for the modelling of the parton shower and using the CUETP8M2T4 underlying event tune [30,31]. In the simulation, the proton structure is described by means of the NNPDF3.0 [32] parton distribution function (PDF) set. The largest background contributions are represented by tW and DY production. Other background processes include W +jets production and diboson events, while the contribution from QCD multi-jet production is found to be negligible. Contributions from all background processes are estimated from simulation and are normalized to their predicted cross section. Further details on the MC simulation of the backgrounds can be found in Ref. [14].

3. Event selection and systematic uncertainties

Events are collected using a combination of triggers which require either one electron with $p_T > 12$ GeV and one muon with

$p_T > 23$ GeV, or one electron with $p_T > 23$ GeV and one muon with $p_T > 8$ GeV, or one electron with $p_T > 27$ GeV, or one muon with $p_T > 24$ GeV. In the analysis, tight isolation requirements are applied to electrons and muons based on the ratio of the scalar sum of the p_T of neighbouring PF candidates to the p_T of the lepton candidate. Events are then required to contain at least one electron and one muon of opposite electric charge with $p_T > 25$ GeV for the leading and $p_T > 20$ GeV for the subleading lepton, and $|\eta| < 2.4$. This kinematic selection defines the visible phase space. In events with more than two leptons, the two leptons of opposite charge with the highest p_T are used. Jets with $p_T > 30$ GeV and $|\eta| < 2.4$ are considered, but no requirement on the number of reconstructed jets or b-tagged jets is imposed. Further details on the event selection can be found in Ref. [14].

In events with at least two jets, the invariant mass of the $t\bar{t}$ system is estimated by means of the kinematic reconstruction algorithm described in Ref. [33]. The reconstructed invariant mass is indicated with $m_{t\bar{t}}^{\text{reco}}$. The kinematic reconstruction algorithm examines all possible combinations of reconstructed jets and leptons and solves a system of equations under the assumptions that the invariant mass of the reconstructed W boson is 80.4 GeV and that the missing transverse momentum originates solely from the two neutrinos coming from the leptonic decays of the W bosons. In addition, the kinematic reconstruction algorithm requires an assumption on the value of the top quark mass, m_t^{kin} . Any possible bias due to the choice of this value is avoided by incorporating the dependence on m_t^{kin} in the fit described in Section 4. To estimate this dependence, the kinematic reconstruction and the event selection are repeated with three different choices of m_t^{kin} , corresponding to 169.5, 172.5, and 175.5 GeV, and the top quark mass used in the MC simulation, m_t^{MC} , is varied accordingly. The parameter $m_t^{\text{kin}} = m_t^{\text{MC}}$ is then treated as a free parameter of the fit.

The sources of systematic uncertainties are classified as experimental and modelling uncertainties. Experimental uncertainties are related to the corrections applied to the MC simulation. These include uncertainties associated with trigger and lepton identification efficiencies, jet energy scale [34] and resolution [35], lepton energy scales, b tagging efficiencies [22], and the uncertainty in the integrated luminosity [36]. Modelling uncertainties are related to the simulation of the $t\bar{t}$ signal, and include matrix-element scale variations in the POWHEG simulation [37,38], scale variations in the parton shower [31], variations in the matching scale between the matrix element and the parton shower [30], uncertainties in the underlying event tune [30], the PDFs [39], the B hadron branching fraction and fragmentation function [40,41], and uncertainties related to the choice of the colour reconnection model [42,43]. Furthermore, as in previous CMS analyses, e.g. [14,44,45], an uncertainty that accounts for the observed difference in the shape of the top quark p_T distribution between data and simulation [33,46,47] is applied. The dependence on the top quark width has been investigated and was found to be negligible. Other sources of uncertainty include the modelling of the additional pp interactions within the same or nearby bunch crossings and the normalization of background processes. For the latter, an uncertainty of 30% is assigned to the normalization of each background process. Further details on the sources of systematic uncertainties and the considered variations can be found in Ref. [14].

The simulated $t\bar{t}$ sample is split into four subsamples corresponding to bins of $m_{t\bar{t}}$ at the parton level. Each subsample is treated as an independent signal process, representing the $t\bar{t}$ production at the scale μ_k , which is chosen to be the centre-of-gravity of bin k , defined as the mean value of $m_{t\bar{t}}$ in that bin. The subsample corresponding to the bin k is denoted with “Signal (μ_k)”. The $m_{t\bar{t}}$ bin boundaries, the corresponding fraction of simulated events in each bin, and the representative scales μ_k are summarized in

Table 1

The $m_{t\bar{t}}$ bin boundaries, the corresponding fraction of events in the POWHEG simulation, and the representative scale μ_k .

Bin	$m_{t\bar{t}}$ [GeV]	Fraction [%]	μ_k [GeV]
1	<420	30	384
2	420–550	39	476
3	550–810	24	644
4	>810	7	1024

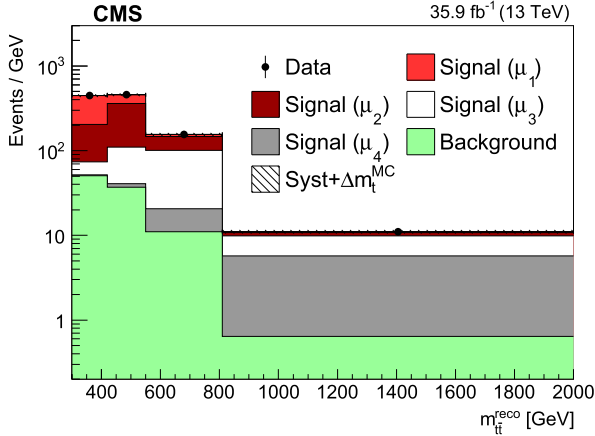


Fig. 1. Distribution of $m_{t\bar{t}}^{\text{reco}}$ after the fit to the data, with the same binning as used in the fit. The hatched band corresponds to the total uncertainty in the predicted yields, including the contribution from m_t^{MC} (Δm_t^{MC}) and all correlations. The $t\bar{t}$ MC sample is split into four subsamples, denoted with “Signal (μ_k)”, corresponding to bins of $m_{t\bar{t}}$ at the parton level. The first and last bins contain all events with $m_{t\bar{t}}^{\text{reco}} < 420$ GeV and $m_{t\bar{t}}^{\text{reco}} > 810$ GeV, respectively.

Table 1, where the values are estimated from the nominal POWHEG simulation. The width of each bin, $\Delta m_{t\bar{t}}^k$, is chosen taking into account the resolution in $m_{t\bar{t}}^{\text{reco}}$. Fig. 1 shows the distribution of $m_{t\bar{t}}^{\text{reco}}$ after the fit to the data, which is described in the next section.

4. Fit procedure and cross section results

The differential $t\bar{t}$ cross section at the parton level is measured by means of a maximum-likelihood fit to distributions of final-state observables where the systematic uncertainties are treated as nuisance parameters. In the likelihood, the number of events in each bin of any distribution of final-state observables is assumed to follow a Poisson distribution. With $\sigma_{t\bar{t}}^{(\mu_k)} = (d\sigma_{t\bar{t}}/dm_{t\bar{t}}) \Delta m_{t\bar{t}}^k$ being the total $t\bar{t}$ cross section in the bin k of $m_{t\bar{t}}$, the expected number of events in the bin i of any of the considered final-state distributions, denoted with ν_i , can be written as

$$\nu_i = \sum_{k=1}^4 s_i^k(\sigma_{t\bar{t}}^{(\mu_k)}, m_t^{\text{MC}}, \vec{\lambda}) + \sum_j b_i^j(m_t^{\text{MC}}, \vec{\lambda}). \quad (2)$$

Here, s_i^k indicates the expected number of $t\bar{t}$ events in the bin k of $m_{t\bar{t}}$ and depends on $\sigma_{t\bar{t}}^{(\mu_k)}$, m_t^{MC} , and the nuisance parameters $\vec{\lambda}$. Similarly, b_i^j represents the expected number of background events from a source j and depends on m_t^{MC} and the nuisance parameters $\vec{\lambda}$. The dependence of the background processes on m_t^{MC} is introduced not only by the contribution of tW and semileptonic $t\bar{t}$ events, but also by the choice of m_t^{kin} in the kinematic reconstruction. Equation (2), which relates the various $\sigma_{t\bar{t}}^{(\mu_k)}$ (and hence the parton-level differential cross section) to distributions of final-state observables, embeds the detector response and its parametrized

dependence on the systematic uncertainties. Therefore, the maximization of the likelihood function provides results for $\sigma_{t\bar{t}}^{(\mu_k)}$ that are automatically unfolded to the parton level. This method (described, e.g. in Ref. [48]) is also referred to as maximum-likelihood unfolding and, unlike other unfolding techniques, allows the nuisance parameters to be constrained simultaneously with the differential cross section. The unfolding problem was found to be well-conditioned, and therefore no regularization is needed. The expected signal and background distributions contributing to the fit are modelled with templates constructed using simulated samples.

Selected events are categorized according to the number of b-tagged jets, as events with 1 b-tagged jet, 2 b-tagged jets, or a different number of b-tagged jets (zero or more than two). The effect of the systematic uncertainties on the normalization of the different signals in each of these categories is parametrized using multinomial probabilities. In particular, based on the $t\bar{t}$ topology, the number of events with one (S_{1b}^k), two (S_{2b}^k), or a different number of b-tagged jets (S_{other}^k) in each bin of $m_{t\bar{t}}$ is expressed as:

$$S_{1b}^k = \mathcal{L} \sigma_{t\bar{t}}^{(\mu_k)} A_{\text{sel}}^k \epsilon_{\text{sel}}^k 2\epsilon_b^k (1 - C_b^k \epsilon_b^k), \quad (3)$$

$$S_{2b}^k = \mathcal{L} \sigma_{t\bar{t}}^{(\mu_k)} A_{\text{sel}}^k \epsilon_{\text{sel}}^k C_b^k (\epsilon_b^k)^2, \quad (4)$$

$$S_{\text{other}}^k = \mathcal{L} \sigma_{t\bar{t}}^{(\mu_k)} A_{\text{sel}}^k \epsilon_{\text{sel}}^k \left[1 - 2\epsilon_b^k (1 - C_b^k \epsilon_b^k) - C_b^k (\epsilon_b^k)^2 \right]. \quad (5)$$

Here, $\mathcal{L}$ is the integrated luminosity, A_{sel}^k is the acceptance of the event selection in the $m_{t\bar{t}}$ bin k , and ϵ_{sel}^k represents the efficiency for an event in the visible phase space to pass the full event selection. The acceptance A_{sel}^k is defined as the fraction of $t\bar{t}$ events in the bin k that, at the generator (particle) level, enter the visible phase space described in Section 3, while ϵ_{sel}^k includes experimental selection criteria, e.g. isolation and trigger requirements. Furthermore, ϵ_b^k represents the b tagging probability and the parameter C_b^k accounts for any residual correlation between the tagging of two b jets in a $t\bar{t}$ event. The quantities A_{sel}^k , ϵ_{sel}^k , ϵ_b^k , and C_b^k are determined from the signal simulation and, although they are not free parameters of the fit, they vary according to the parameters $\vec{\lambda}$ and m_t^{MC} . In each category, the remaining effects of the systematic uncertainties on signal processes are treated as shape uncertainties. The quantities s_i^k in Eq. (2) are then derived from the signal shape and normalization in the corresponding category. In this way, a precise parametrization of the dependence of signal normalizations on the nuisance parameters and m_t^{MC} is obtained. In fact, the parameters in Eqs. (3)–(5) are less subject to statistical fluctuations than the s_i^k .

In order to constrain each individual $\sigma_{t\bar{t}}^{(\mu_k)}$, events with at least two jets are further divided into subcategories of $m_{t\bar{t}}^{\text{reco}}$, using the same binning as for $m_{t\bar{t}}$ (Table 1). The choice of the input distributions to the fit in the different event categories is summarized in Table 2. The total number of events is chosen as input to the fit for all subcategories with zero or more than two b-tagged jets, where the contribution of the background processes is the largest, in order to mitigate the sensitivity of the measurement to the shape of the distributions of background processes. The same choice is made for the subcategories corresponding to the last bin in $m_{t\bar{t}}^{\text{reco}}$, where the statistical uncertainty in both data and simulation is large, and for events with less than two jets, where the kinematic reconstruction cannot be performed. In the remaining subcategories with one b-tagged jet, the minimum invariant mass found when combining the reconstructed b jet and a lepton, referred to as the $m_{b\ell}^{\text{min}}$ distribution, is fitted. This distribution provides the

Table 2

Input distributions to the fit in the different event categories. The number of jets, the number of b-tagged jets, the number of events, and the p_T of the softest jet are denoted with N_{jets} , N_b , N_{events} , and “jet p_T^{min} ”, respectively, while the category corresponding to the bin k in $m_{\text{tt}}^{\text{reco}}$ is indicated with “ $m_{\text{tt}}^{\text{reco}} k$ ”.

	$N_b = 1$	$N_b = 2$	Other N_b
$N_{\text{jets}} < 2$	N_{events}	n.a.	N_{events}
$m_{\text{tt}}^{\text{reco}} 1$	$m_{\text{lb}}^{\text{min}}$	jet p_T^{min}	N_{events}
$m_{\text{tt}}^{\text{reco}} 2$	$m_{\text{lb}}^{\text{min}}$	jet p_T^{min}	N_{events}
$m_{\text{tt}}^{\text{reco}} 3$	$m_{\text{lb}}^{\text{min}}$	jet p_T^{min}	N_{events}
$m_{\text{tt}}^{\text{reco}} 4$	N_{events}	N_{events}	N_{events}

sensitivity to constrain m_{t}^{MC} [49]. In the remaining subcategories with two b-tagged jets, the p_T spectrum of the softest selected jet in the event is used to constrain jet energy scale uncertainties at small values of p_T , the kinematic range where systematic uncertainties are the largest. The distributions used in the fit are compared to the data after the fit in the supplemental material.

The efficiencies of the kinematic reconstruction in data and simulation have been investigated in Ref. [33] and they were found to differ by 0.2%. Therefore, the efficiency in the simulation is corrected to match the one in data. An uncertainty of 0.2% is assigned to each bin of m_{tt} independently. The same uncertainty is also assigned to tt events with one or two b-tagged jets, independently. For tt events with zero or more than two b-tagged jets, where the combinatorial background is larger, an uncertainty of 0.5% is conservatively assigned. These uncertainties are treated as uncorrelated to account for possible differences between the different m_{tt} bins and categories of b-tagged jet multiplicity. Similarly, an additional uncertainty of 1% is assigned to the sum of the background processes, independently for each bin of $m_{\text{tt}}^{\text{reco}}$, in order to reduce the correlation between the signal and the background templates. The impact of these uncertainties on the final results is found to be small compared to the total uncertainty.

The dependence of the signal shapes, of the parameters A_{sel}^k , ϵ_{sel}^k , ϵ_b^k , and C_b^k , and of the background contributions on m_{t}^{MC} and on the nuisance parameters $\vec{\lambda}$ is modelled using second-order polynomials [14]. In the fit, Gaussian priors are assumed for all the nuisance parameters. The negative log-likelihood is then minimized, using the MINUIT program [50], with respect to $\sigma_{\text{tt}}^{(\mu_k)}$, m_{t}^{MC} , and $\vec{\lambda}$. Finally, the fit uncertainties in the various $\sigma_{\text{tt}}^{(\mu_k)}$ are determined using MINOS [50]. Additional extrapolation uncertainties, which reflect the impact of modelling uncertainties on A_{sel}^k , are estimated without taking into account the constraints obtained in the visible phase space [14]. Moreover, an additional uncertainty arising from the limited statistical precision of the simulation is estimated using MC pseudo-experiments [14], where templates are varied within their statistical uncertainties taking into account the correlations between the nominal templates and the templates corresponding to the systematic variations. The template dependencies are then rederived and the fit to the data is repeated more than ten thousand times. For each parameter of interest, the root-mean-square of the best fit values obtained with this procedure is taken as an additional uncertainty and added in quadrature to the total uncertainty from the fit.

The measured $\sigma_{\text{tt}}^{(\mu_k)}$ are shown in Fig. 2 and compared to fixed-order theoretical predictions in the $\overline{\text{MS}}$ scheme at NLO [51] implemented for the purpose of this analysis in the MCFM v6.8 program [52,53]. In the calculation, the renormalization scale, μ_r , and factorization scale, μ_f , are both set to m_{t} . The $\overline{\text{MS}}$ mass of the top quark evaluated at the scale $\mu = m_{\text{t}}$ is denoted with $m_{\text{t}}(m_{\text{t}})$.

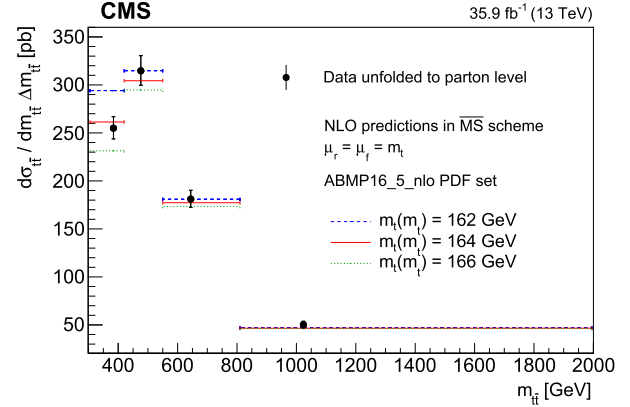


Fig. 2. Measured values of $\sigma_{\text{tt}}^{(\mu_k)}$ (markers) and their uncertainties (vertical error bars) compared to NLO predictions in the $\overline{\text{MS}}$ scheme obtained with different values of $m_{\text{t}}(m_{\text{t}})$ (horizontal lines of different styles). The values of $\sigma_{\text{tt}}^{(\mu_k)}$ are shown at the representative scale of the process μ_k , defined as the centre-of-gravity of bin k in m_{tt} . The first and last bins contain all events with $m_{\text{tt}} < 420 \text{ GeV}$ and $m_{\text{tt}} > 810 \text{ GeV}$, respectively.

The calculation is interfaced with the ABMP16_5_nlo PDF set [54], which is the only available PDF set where m_{t} is treated in the $\overline{\text{MS}}$ scheme and where the correlations between the gluon PDF, α_s , and m_{t} are taken into account. In the calculation, the value of α_s at the Z boson mass, $\alpha_s(m_Z)$, is set to the value determined in the ABMP16_5_nlo fit, which in the central PDF corresponds to 0.1191 [54]. In order to demonstrate the sensitivity to the top quark mass, predictions for $d\sigma_{\text{tt}}/dm_{\text{tt}}$ obtained with different values of $m_{\text{t}}(m_{\text{t}})$ are shown. Furthermore, it is worth noting that this method provides a cross section result with significantly improved precision compared to measurements that perform unfolding as a separate step, e.g. as the one described in Ref. [33].

The dominant uncertainties in the measured $\sigma_{\text{tt}}^{(\mu_k)}$ are associated with the integrated luminosity, the lepton identification efficiencies, the jet energy scales and, at large m_{tt} , the modelling of the top quark p_T . The two latter uncertainties are marginally constrained in the fit, while the first two are not constrained. Furthermore, the post-fit values of all nuisance parameters are found to be compatible with their pre-fit value, within one standard deviation. The numerical values of the measured $\sigma_{\text{tt}}^{(\mu_k)}$, their correlations, the impact of the various sources of uncertainty, and the pulls and constraints of the nuisance parameters related to the modelling uncertainties can be found in the supplemental material.

5. Extraction of the running of the top quark mass

The measured differential cross section is used to extract the running of the top quark $\overline{\text{MS}}$ mass at NLO as a function of the scale $\mu = m_{\text{tt}}$. The procedure is similar to the one used to extract the running of the charm quark mass [12]. The value of $m_{\text{t}}(m_{\text{t}})$ is determined independently in each bin of m_{tt} from a χ^2 fit of fixed-order theoretical predictions at NLO to the measured $\sigma_{\text{tt}}^{(\mu_k)}$. The theoretical predictions are obtained as described in Section 4 for Fig. 2. The χ^2 definition follows the one described in Ref. [55], which accounts for asymmetries in the input uncertainties. The extracted $m_{\text{t}}(m_{\text{t}})$ are then converted to $m_{\text{t}}(\mu_k)$ using the CRUNDEC v3.0 program [56], where μ_k is the representative scale of the process in a given bin of m_{tt} , as described in Section 3. As relevant in a NLO calculation, the conversion is performed with one-loop precision, assuming five active flavours ($n_f = 5$) and $\alpha_s(m_Z) = 0.1191$ consistently with the used PDF set. This procedure is equivalent to extracting directly $m_{\text{t}}(\mu_k)$ in each bin. Furthermore, the result does not depend on the exact choice of

μ_k , provided that it is representative of the physical energy scale of the process. In fact, a change in μ_k would correspond to a change in $m_t(\mu_k)$ according to the RGE. The extracted values of $m_t(\mu_k)$ and their uncertainties can be found in the supplemental material.

In order to benefit from the cancellation of correlated uncertainties in the measured $\sigma_{tt}^{(\mu_k)}$, the ratios of the various $m_t(\mu_k)$ to $m_t(\mu_2)$ are considered. In particular, the quantities $r_{12} = m_t(\mu_1)/m_t(\mu_2)$, $r_{32} = m_t(\mu_3)/m_t(\mu_2)$, and $r_{42} = m_t(\mu_4)/m_t(\mu_2)$ are extracted. With this approach the running of m_t , i.e. the quantity predicted by the RGE (Eq. (1)), is accessed directly. The measurement at the scale μ_2 is chosen as a reference in order to minimize the correlation between the extracted ratios.

Four different types of systematic uncertainty are considered for the ratios: the uncertainty in the various $\sigma_{tt}^{(\mu_k)}$ in the visible phase space (referred to as fit uncertainty), the extrapolation uncertainties, the uncertainties in the proton PDFs, and the uncertainty in the value of $\alpha_s(m_Z)$. The fit uncertainty includes experimental and modelling uncertainties described in Section 3. Scale variations in the MCFM predictions are not performed, since the scale dependence of m_t is being investigated at a fixed order in perturbation theory. In fact, scale variations in the hard scattering cross section are conventionally performed as a means of estimating the effect of missing higher order corrections and are therefore not applicable in this context.

Uncertainties in the proton PDFs affect the MCFM prediction and therefore the extracted values of the various $m_t(\mu_k)$. In order to estimate their impact, the calculation is repeated for each eigenvector of the PDF set and the differences in the extracted ratios are added in quadrature to yield the total PDF uncertainties. In the ABMP16_5_nlo PDF set, $\alpha_s(m_Z)$ is determined simultaneously with the PDFs, therefore its uncertainty is incorporated in that of the PDFs. However, the uncertainty in $\alpha_s(m_Z)$ also affects the CRUNDEC conversion from $m_t(m_t)$ to $m_t(\mu_k)$. This effect is estimated independently and is found to be negligible.

The impact of extrapolation uncertainties is estimated by varying the measured $\sigma_{tt}^{(\mu_k)}$ within their extrapolation uncertainty, separately for each source and simultaneously in the different bins in m_{tt} , taking the correlations into account. The various contributions are added in quadrature to yield the total extrapolation uncertainty.

The correlations between the extracted masses arising from the fit uncertainty are estimated using MC pseudo-experiments, taking the correlations between the measured $\sigma_{tt}^{(\mu_k)}$ as inputs. The uncertainties are then propagated to the ratios using linear uncertainty propagation, taking the estimated correlations into account. The numerical values of the ratios are determined to be:

$$\begin{aligned} r_{12} &= 1.030 \pm 0.018 \text{ (fit)} \begin{smallmatrix} +0.003 \\ -0.006 \end{smallmatrix} \text{ (PDF+}\alpha_s) \begin{smallmatrix} +0.003 \\ -0.002 \end{smallmatrix} \text{ (extr)}, \\ r_{32} &= 0.982 \pm 0.025 \text{ (fit)} \begin{smallmatrix} +0.006 \\ -0.005 \end{smallmatrix} \text{ (PDF+}\alpha_s) \pm 0.004 \text{ (extr)}, \\ r_{42} &= 0.904 \pm 0.050 \text{ (fit)} \begin{smallmatrix} +0.019 \\ -0.017 \end{smallmatrix} \text{ (PDF+}\alpha_s) \begin{smallmatrix} +0.017 \\ -0.013 \end{smallmatrix} \text{ (extr)}. \end{aligned}$$

Here, the fit uncertainty (fit), the combination of PDF and α_s uncertainty (PDF+ α_s), and the extrapolation uncertainty (extr) are given. The most relevant sources of experimental uncertainty are the integrated luminosity, the lepton identification efficiencies, and the jet energy scale and resolution. Among modelling uncertainties related to the POWHEG+PYTHIA 8 simulation of the $t\bar{t}$ signal, the largest contributions originate from the scale variations in the parton shower, the uncertainty in the shape of the p_T spectrum of the top quark, and the matching scale between the matrix element and the parton shower. The statistical uncertainties are found to be negligible. The correlations between the ratios arising from the fit uncertainty are investigated using a pseudo-experiment procedure which consists in repeating the extraction of the ratios using

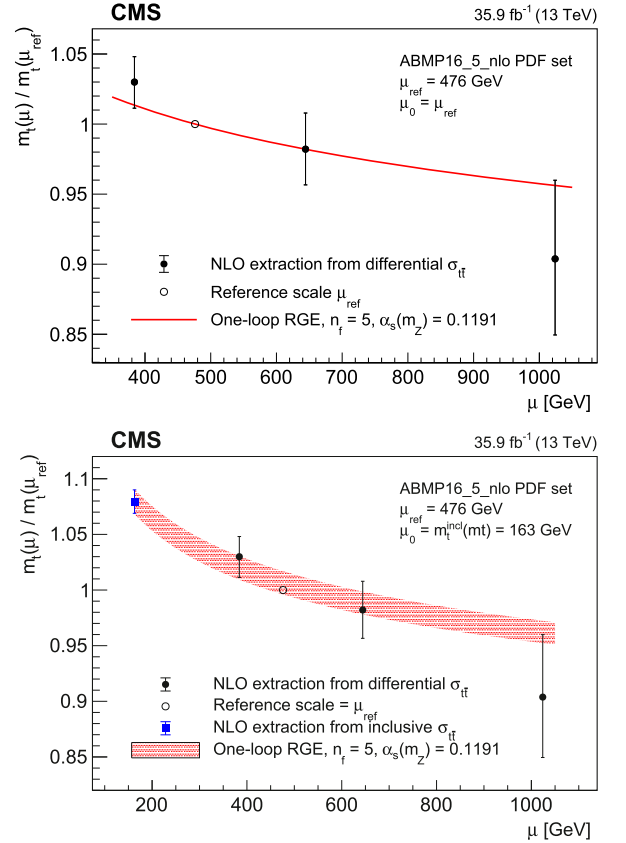


Fig. 3. Extracted running of the top quark mass $m_t(\mu)/m_t(\mu_{\text{ref}})$ compared to the RGE prediction at one-loop precision, with $n_f = 5$, evolved from the initial scale $\mu_0 = \mu_{\text{ref}} = 476 \text{ GeV}$ (upper). The result is compared to the value of $m_t^{\text{incl}}(m_t)/m_t(\mu_{\text{ref}})$, where $m_t^{\text{incl}}(m_t)$ is the value of $m_t(m_t)$ extracted from the inclusive cross section measured in Ref. [14], which is based on the same data set. The uncertainty in $m_t^{\text{incl}}(m_t)$ is evolved from the initial scale $\mu_0 = m_t^{\text{incl}}(m_t)$, which corresponds to about 163 GeV, using the same RGE prediction (lower).

pseudo-measurements of $\sigma_{tt}^{(\mu_k)}$, generated according to the corresponding fitted values, uncertainties, and correlations. With ρ_{ik} being the correlation between r_{i2} and r_{k2} , the results are $\rho_{13} = 13\%$, $\rho_{14} = -45\%$, and $\rho_{34} = 11\%$.

The extracted ratios $m_t(\mu_k)/m_t(\mu_2)$ are shown in Fig. 3 (upper) together with the RGE prediction (Eq. (1)) at one-loop precision. In the figure, the reference scale μ_2 is indicated with μ_{ref} , and the RGE evolution is calculated from the initial scale $\mu_0 = \mu_{\text{ref}}$. Good agreement between the extracted running and the RGE prediction is observed.

For comparison, the $\overline{MS}$ mass of the top quark is also extracted from the inclusive cross section measured in Ref. [14], using HATHOR 2.0 [57] predictions at NLO interfaced with the ABMP16_5_nlo PDF set, and is denoted with $m_t^{\text{incl}}(m_t)$. Fig. 3 (lower) compares the extracted ratios $m_t(\mu_k)/m_t(\mu_2)$ to the value of $m_t^{\text{incl}}(m_t)/m_t(\mu_2)$. The uncertainty in $m_t^{\text{incl}}(m_t)$ includes fit, extrapolation, and PDF uncertainties, and is evolved to higher scales, while the value of $m_t(\mu_2)$ in the ratio $m_t^{\text{incl}}(m_t)/m_t(\mu_2)$ is taken without uncertainty. Here, the RGE evolution is calculated from the initial scale $\mu_0 = m_t^{\text{incl}}(m_t)$, which corresponds to about 163 GeV. The extracted value of $m_t^{\text{incl}}(m_t)$ and its uncertainty can be found in the supplemental material.

Finally, the extracted running is parametrized with the function

$$f(x, \mu) = x[r(\mu) - 1] + 1, \quad (6)$$

where $r(\mu) = m_t(\mu)/m_t(\mu_2)$ corresponds to the RGE prediction shown in Fig. 3 (upper). In particular, $f(x, \mu)$ corresponds to

$r(\mu)$ for $x = 1$ and to 1, i.e. no running, for $x = 0$. The best fit value for x , denoted with $\hat{x}$, is determined via a χ^2 fit to the extracted ratios taking the correlations ρ_{ik} into account, and is found to be

$$\hat{x} = 2.05 \pm 0.61 \text{ (fit)} \stackrel{+0.31}{-0.55} \text{ (PDF} + \alpha_S) \stackrel{+0.24}{-0.49} \text{ (extr).}$$

The result shows agreement between the extracted running and the RGE prediction at one-loop precision within 1.1 standard deviations in the Gaussian approximation and excludes the no-running hypothesis at above 95% confidence level (2.1 standard deviations) in the same approximation.

6. Summary

In this Letter, the first experimental investigation of the running of the top quark mass, m_t , is presented. The running is extracted from a measurement of the differential top quark-antiquark ($t\bar{t}$) cross section as a function of the invariant mass of the $t\bar{t}$ system, $m_{t\bar{t}}$. The differential $t\bar{t}$ cross section, $d\sigma_{t\bar{t}}/dm_{t\bar{t}}$, is determined at the parton level using a maximum-likelihood fit to distributions of final-state observables, using $t\bar{t}$ candidate events in the $e^\pm\mu^\mp$ channel. This technique allows the nuisance parameters to be constrained simultaneously with the differential cross section in the visible phase space and therefore provides results with significantly improved precision compared to conventional procedures in which the unfolding is performed as a separate step. The analysis is performed using proton-proton collision data at a centre-of-mass energy of 13 TeV recorded by the CMS detector at the CERN LHC in 2016, corresponding to an integrated luminosity of 35.9 fb^{-1} .

The running mass $m_t(\mu)$, as defined in the modified minimal subtraction ($\overline{\text{MS}}$) renormalization scheme, is extracted at one-loop precision as a function of $m_{t\bar{t}}$ by comparing fixed-order theoretical predictions at next-to-leading order to the measured $d\sigma_{t\bar{t}}/dm_{t\bar{t}}$. The extracted running of m_t is found to be in agreement with the prediction of the corresponding renormalization group equation, within 1.1 standard deviations, and the no-running hypothesis is excluded at above 95% confidence level. The running of m_t is probed up to a scale of the order of 1 TeV.

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Appendix A. Supplementary material

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References

- [1] A. Deur, S.J. Brodsky, G.F. de Teramond, The QCD running coupling, *Prog. Part. Nucl. Phys.* 90 (2016) 1, <https://doi.org/10.1016/j.pnpnp.2016.04.003>, arXiv:1604.08082.
- [2] CMS Collaboration, Measurement and QCD analysis of double-differential inclusive jet cross sections in pp collisions at $\sqrt{s} = 8 \text{ TeV}$ and cross section ratios to 2.76 and 7 TeV, *J. High Energy Phys.* 03 (2017) 156, [https://doi.org/10.1007/JHEP03\(2017\)156](https://doi.org/10.1007/JHEP03(2017)156), arXiv:1609.05331.
- [3] P.A. Baikov, K.G. Chetyrkin, J.H. Kühn, Quark mass and field anomalous dimensions to $\mathcal{O}(\alpha_s^3)$, *J. High Energy Phys.* 10 (2014) 076, [https://doi.org/10.1007/JHEP10\(2014\)076](https://doi.org/10.1007/JHEP10(2014)076), arXiv:1402.6611.
- [4] T. Luthe, A. Maier, P. Marquard, Y. Schröder, Five-loop quark mass and field anomalous dimensions for a general gauge group, *J. High Energy Phys.* 01 (2017) 081, [https://doi.org/10.1007/JHEP01\(2017\)081](https://doi.org/10.1007/JHEP01(2017)081), arXiv:1612.05512.
- [5] O. Behnke, A. Geiser, M. Lisovsky, Charm, beauty and top at HERA, *Prog. Part. Nucl. Phys.* 84 (2015) 1, <https://doi.org/10.1016/j.pnpnp.2015.06.002>, arXiv:1506.07519.
- [6] J. Abdallah, et al., DELPHI, Study of b-quark mass effects in multijet topologies with the DELPHI detector at LEP, *Eur. Phys. J. C* 55 (2008) 525, <https://doi.org/10.1140/epjc/s10052-008-0631-5>, arXiv:0804.3883.
- [7] J. Abdallah, et al., DELPHI, Determination of the b quark mass at the M_Z scale with the DELPHI detector at LEP, *Eur. Phys. J. C* 46 (2006) 569, <https://doi.org/10.1140/epjc/s2006-02497-6>.
- [8] R. Barate, et al., ALEPH, A measurement of the b quark mass from hadronic Z decays, *Eur. Phys. J. C* 18 (2000) 1, <https://doi.org/10.1007/s100520000533>, arXiv:hep-ex/0008013.

- [9] G. Abbiendi, et al., OPAL, Determination of the b quark mass at the Z mass scale, *Eur. Phys. J. C* 21 (2001) 411, <https://doi.org/10.1007/s100520100746>, arXiv:hep-ex/0105046.
- [10] A. Brandenburg, P.N. Burrows, D. Muller, N. Oishi, P. Uwer, Measurement of the running b quark mass using $e^+e^- \rightarrow b\bar{b}g$ events, *Phys. Lett. B* 468 (1999) 168, [https://doi.org/10.1016/S0370-2693\(99\)01194-6](https://doi.org/10.1016/S0370-2693(99)01194-6), arXiv:hep-ph/9905495.
- [11] H. Abramowicz, et al., ZEUS, Measurement of beauty and charm production in deep inelastic scattering at HERA and measurement of the beauty-quark mass, *J. High Energy Phys.* 09 (2014) 127, [https://doi.org/10.1007/JHEP09\(2014\)127](https://doi.org/10.1007/JHEP09(2014)127), arXiv:1405.6915.
- [12] A. Gizhko, et al., Running of the charm-quark mass from HERA deep-inelastic scattering data, *Phys. Lett. B* 775 (2017) 233, <https://doi.org/10.1016/j.physletb.2017.11.002>, arXiv:1705.08863.
- [13] L. Mihaila, Precision calculations in supersymmetric theories, *Adv. High Energy Phys.* 2013 (2013) 607807, <https://doi.org/10.1155/2013/607807>, arXiv:1310.6178.
- [14] CMS Collaboration, Measurement of the $t\bar{t}$ production cross section, the top quark mass, and the strong coupling constant using dilepton events in pp collisions at $\sqrt{s} = 13$ TeV, *Eur. Phys. J. C* 79 (2019) 368, <https://doi.org/10.1140/epjc/s10052-019-6863-8>, arXiv:1812.10505.
- [15] CMS Collaboration, The CMS trigger system, *J. Instrum.* 12 (2017) P01020, <https://doi.org/10.1088/1748-0221/12/01/P01020>, arXiv:1609.02366.
- [16] CMS Collaboration, The CMS experiment at the CERN LHC, *J. Instrum.* 3 (2008) S08004, <https://doi.org/10.1088/1748-0221/3/08/S08004>.
- [17] CMS Collaboration, Particle-flow reconstruction and global event description with the CMS detector, *J. Instrum.* 12 (2017) P10003, <https://doi.org/10.1088/1748-0221/12/10/P10003>, arXiv:1706.04965.
- [18] CMS Collaboration, Performance of electron reconstruction and selection with the CMS detector in proton-proton collisions at $\sqrt{s} = 8$ TeV, *J. Instrum.* 10 (2015) P06005, <https://doi.org/10.1088/1748-0221/10/06/P06005>, arXiv:1502.02701.
- [19] CMS Collaboration, Performance of the CMS muon detector and muon reconstruction with proton-proton collisions at $\sqrt{s} = 13$ TeV, *J. Instrum.* 13 (2018) P06015, <https://doi.org/10.1088/1748-0221/13/06/P06015>, arXiv:1804.04528.
- [20] M. Cacciari, G.P. Salam, G. Soyez, The anti- k_T jet clustering algorithm, *J. High Energy Phys.* 04 (2008) 063, <https://doi.org/10.1088/1126-6708/2008/04/063>, arXiv:0802.1189.
- [21] M. Cacciari, G.P. Salam, G. Soyez, FastJet user manual, *Eur. Phys. J. C* 72 (2012) 1896, <https://doi.org/10.1140/epjc/s10052-012-1896-2>, arXiv:1111.6097.
- [22] CMS Collaboration, Identification of heavy-flavour jets with the CMS detector in pp collisions at 13 TeV, *J. Instrum.* 13 (2018) P05011, <https://doi.org/10.1088/1748-0221/13/05/P05011>, arXiv:1712.07158.
- [23] P. Nason, A new method for combining NLO QCD with shower Monte Carlo algorithms, *J. High Energy Phys.* 11 (2004) 040, <https://doi.org/10.1088/1126-6708/2004/11/040>, arXiv:hep-ph/0409146.
- [24] S. Frixione, P. Nason, C. Oleari, Matching NLO QCD computations with parton shower simulations: the POWHEG method, *J. High Energy Phys.* 11 (2007) 070, <https://doi.org/10.1088/1126-6708/2007/11/070>, arXiv:0709.2092.
- [25] S. Alioli, P. Nason, C. Oleari, E. Re, A general framework for implementing NLO calculations in shower Monte Carlo programs: the POWHEG BOX, *J. High Energy Phys.* 06 (2010) 043, [https://doi.org/10.1007/JHEP06\(2010\)043](https://doi.org/10.1007/JHEP06(2010)043), arXiv:1002.2581.
- [26] S. Frixione, P. Nason, G. Ridolfi, A positive-weight next-to-leading-order Monte Carlo for heavy flavour hadroproduction, *J. High Energy Phys.* 09 (2007) 126, <https://doi.org/10.1088/1126-6708/2007/09/126>, arXiv:0707.3088.
- [27] E. Re, Single-top Wt-channel production matched with parton showers using the POWHEG method, *Eur. Phys. J. C* 71 (2011) 1547, <https://doi.org/10.1140/epjc/s10052-011-1547-z>, arXiv:1009.2450.
- [28] S. Alioli, P. Nason, C. Oleari, E. Re, Vector boson plus one jet production in POWHEG, *J. High Energy Phys.* 01 (2011) 095, [https://doi.org/10.1007/JHEP01\(2011\)095](https://doi.org/10.1007/JHEP01(2011)095), arXiv:1009.5594.
- [29] T. Sjöstrand, S. Ask, J.R. Christiansen, R. Corke, N. Desai, P. Ilten, S. Mrenna, S. Prestel, C.O. Rasmussen, P.Z. Skands, An introduction to PYTHIA 8.2, *Comput. Phys. Commun.* 191 (2015) 159, <https://doi.org/10.1016/j.cpc.2015.01.024>, arXiv:1410.3012.
- [30] CMS Collaboration, Investigations of the impact of the parton shower tuning in PYTHIA 8 in the modelling of $t\bar{t}$ at $\sqrt{s} = 8$ and 13 TeV, CMS Physics Analysis Summary CMS-PAS-TOP-16-021, 2016, <https://cds.cern.ch/record/2235192>.
- [31] P. Skands, S. Carrazza, J. Rojo, Tuning PYTHIA 8.1: the Monash 2013 tune, *Eur. Phys. J. C* 74 (2014) 3024, <https://doi.org/10.1140/epjc/s10052-014-3024-y>, arXiv:1404.5630.
- [32] R.D. Ball, et al., NNPDF, Parton distributions for the LHC Run II, *J. High Energy Phys.* 04 (2015) 040, [https://doi.org/10.1007/JHEP04\(2015\)040](https://doi.org/10.1007/JHEP04(2015)040), arXiv:1410.8849.
- [33] CMS Collaboration, Measurements of $t\bar{t}$ differential cross sections in proton-proton collisions at $\sqrt{s} = 13$ TeV using events containing two leptons, *J. High Energy Phys.* 02 (2019) 149, [https://doi.org/10.1007/JHEP02\(2019\)149](https://doi.org/10.1007/JHEP02(2019)149), arXiv:1811.06625.
- [34] CMS Collaboration, Jet energy scale and resolution in the CMS experiment in pp collisions at 8 TeV, *J. Instrum.* 12 (2017) P02014, <https://doi.org/10.1088/1748-0221/12/02/P02014>, arXiv:1607.03663.
- [35] CMS Collaboration, Jet algorithms performance in 13 TeV data, CMS Physics Analysis Summary CMS-PAS-JME-16-003, 2017, <http://cds.cern.ch/record/2256875>.
- [36] CMS Collaboration, CMS luminosity measurements for the 2016 data taking period, CMS Physics Analysis Summary CMS-PAS-LUM-17-001, 2017, <http://cds.cern.ch/record/2257069>.
- [37] M. Cacciari, S. Frixione, M.L. Mangano, P. Nason, G. Ridolfi, The $t\bar{t}$ cross-section at 1.8 TeV and 1.96 TeV: a study of the systematics due to parton densities and scale dependence, *J. High Energy Phys.* 04 (2004) 068, <https://doi.org/10.1088/1126-6708/2004/04/068>, arXiv:hep-ph/0303085.
- [38] S. Catani, D. de Florian, M. Grazzini, P. Nason, Soft gluon resummation for Higgs boson production at hadron colliders, *J. High Energy Phys.* 07 (2003) 028, <https://doi.org/10.1088/1126-6708/2003/07/028>, arXiv:hep-ph/0306211.
- [39] S. Dulat, T.-J. Hou, J. Gao, M. Guzzi, J. Huston, P. Nadolsky, J. Pumplin, C. Schmidt, D. Stump, C.P. Yuan, New parton distribution functions from a global analysis of quantum chromodynamics, *Phys. Rev. D* 93 (2016) 033006, <https://doi.org/10.1103/PhysRevD.93.033006>, arXiv:1506.07443.
- [40] M.G. Bowler, e^+e^- production of heavy quarks in the string model, *Z. Phys. C* 11 (1981) 169, <https://doi.org/10.1007/BF01574001>.
- [41] C. Peterson, D. Schlatter, I. Schmitt, P.M. Zerwas, Scaling violations in inclusive e^+e^- annihilation spectra, *Phys. Rev. D* 27 (1983) 105, <https://doi.org/10.1103/PhysRevD.27.105>.
- [42] S. Argyropoulos, T. Sjöstrand, Effects of color reconnection on $t\bar{t}$ final states at the LHC, *J. High Energy Phys.* 11 (2014) 043, [https://doi.org/10.1007/JHEP11\(2014\)043](https://doi.org/10.1007/JHEP11(2014)043), arXiv:1407.6653.
- [43] J.R. Christiansen, P.Z. Skands, String formation beyond leading colour, *J. High Energy Phys.* 08 (2015) 003, [https://doi.org/10.1007/JHEP08\(2015\)003](https://doi.org/10.1007/JHEP08(2015)003), arXiv:1505.01681.
- [44] CMS Collaboration, Measurement of the top quark Yukawa coupling from $t\bar{t}$ kinematic distributions in the lepton+jets final state in proton-proton collisions at $\sqrt{s} = 13$ TeV, *Phys. Rev. D* 100 (2019) 072007, <https://doi.org/10.1103/PhysRevD.100.072007>, arXiv:1907.01590.
- [45] CMS Collaboration, Measurement of the top quark polarization and $t\bar{t}$ spin correlations using dilepton final states in proton-proton collisions at $\sqrt{s} = 13$ TeV, *Phys. Rev. D* 100 (2019) 072002, <https://doi.org/10.1103/PhysRevD.100.072002>, arXiv:1907.03729.
- [46] CMS Collaboration, Measurement of normalized differential $t\bar{t}$ cross sections in the dilepton channel from pp collisions at $\sqrt{s} = 13$ TeV, *J. High Energy Phys.* 04 (2018) 060, [https://doi.org/10.1007/JHEP04\(2018\)060](https://doi.org/10.1007/JHEP04(2018)060), arXiv:1708.07638.
- [47] CMS Collaboration, Measurement of differential cross sections for top quark pair production using the lepton+jets final state in proton-proton collisions at 13 TeV, *Phys. Rev. D* 95 (2017) 092001, <https://doi.org/10.1103/PhysRevD.95.092001>, arXiv:1610.04191.
- [48] CMS Collaboration, Measurement of inclusive and differential Higgs boson production cross sections in the diphoton decay channel in proton-proton collisions at $\sqrt{s} = 13$ TeV, *J. High Energy Phys.* 01 (2019) 183, [https://doi.org/10.1007/JHEP01\(2019\)183](https://doi.org/10.1007/JHEP01(2019)183), arXiv:1807.03825.
- [49] S. Biswas, K. Melnikov, M. Schulze, Next-to-leading order QCD effects and the top quark mass measurements at the LHC, *J. High Energy Phys.* 08 (2010) 048, [https://doi.org/10.1007/JHEP08\(2010\)048](https://doi.org/10.1007/JHEP08(2010)048), arXiv:1006.0910.
- [50] F. James, M. Roos, MINUIT: a system for function minimization and analysis of the parameter errors and correlations, *Comput. Phys. Commun.* 10 (1975) 343, [https://doi.org/10.1016/0010-4655\(75\)90039-9](https://doi.org/10.1016/0010-4655(75)90039-9).
- [51] M. Dowling, S.-O. Moch, Differential distributions for top-quark hadroproduction with a running mass, *Eur. Phys. J. C* 74 (2014) 3167, <https://doi.org/10.1140/epjc/s10052-014-3167-x>, arXiv:1305.6422.
- [52] J.M. Campbell, R.K. Ellis, MCFM for the Tevatron and the LHC, *Nucl. Phys. B, Proc. Suppl.* 205–206 (2010) 10, <https://doi.org/10.1016/j.nuclphysbbs.2010.08.011>, arXiv:1007.3492.
- [53] J.M. Campbell, R.K. Ellis, Top-quark processes at NLO in production and decay, *J. Phys. G* 42 (2015) 015005, <https://doi.org/10.1088/0954-3899/42/1/015005>, arXiv:1204.1513.
- [54] S. Alekhin, J. Blümlein, S. Moch, NLO PDFs from the ABMP16 fit, *Eur. Phys. J. C* 78 (2018) 477, <https://doi.org/10.1140/epjc/s10052-018-5947-1>, arXiv:1803.07537.
- [55] R. Barlow, Asymmetric errors, in: *Statistical Problems in Particle Physics, Astrophysics and Cosmology, Proceedings, Conference, PHYSTAT 2003, Stanford, USA, 2003*, p. WEMT002, arXiv:physics/0401042, eConf C030908.
- [56] B. Schmidt, M. Steinhauser, CRUDer: a C++ package for running and decoupling of the strong coupling and quark masses, *Comput. Phys. Commun.* 183 (2012) 1845, <https://doi.org/10.1016/j.cpc.2012.03.023>, arXiv:1201.6149.
- [57] M. Aliev, H. Lacker, U. Langenfeld, S. Moch, P. Uwer, M. Wiedermann, HATHOR: Hadronic top and heavy quarks crOSS section calculator, *Comput. Phys. Commun.* 182 (2011) 1034, <https://doi.org/10.1016/j.cpc.2010.12.040>, arXiv:1007.1327.

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